

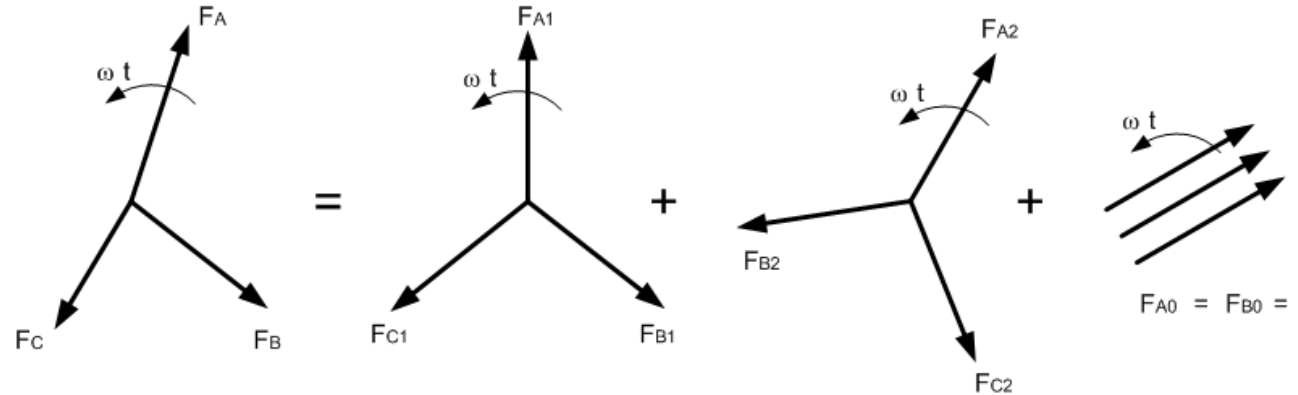
Symmetrical system components

Decomposition of unsymmetrical (unbalanced) voltage:

$$\hat{U}_A = \hat{U}_{A1} + \hat{U}_{A2} + \hat{U}_{A0}$$

$$\hat{U}_B = \hat{U}_{B1} + \hat{U}_{B2} + \hat{U}_{B0}$$

$$\hat{U}_C = \hat{U}_{C1} + \hat{U}_{C2} + \hat{U}_{C0}$$



Positive sequence (1), negative (2) and zero (0) sequence.

Hence (reference phase A)

$$\hat{U}_A = \hat{U}_1 + \hat{U}_2 + \hat{U}_0$$

$$\hat{U}_B = \hat{a}^2 \hat{U}_1 + \hat{a} \hat{U}_2 + \hat{U}_0$$

$$\hat{U}_C = \hat{a} \hat{U}_1 + \hat{a}^2 \hat{U}_2 + \hat{U}_0$$

$$\hat{I}_A = \hat{I}_1 + \hat{I}_2 + \hat{I}_0$$

$$\hat{I}_B = \hat{a}^2 \hat{I}_1 + \hat{a} \hat{I}_2 + \hat{I}_0$$

$$\hat{I}_C = \hat{a} \hat{I}_1 + \hat{a}^2 \hat{I}_2 + \hat{I}_0$$

where $\hat{a} = -\frac{1}{2} + j\frac{\sqrt{3}}{2} = e^{j\frac{2\pi}{3}}$

$$\hat{a}^2 = -\frac{1}{2} - j\frac{\sqrt{3}}{2} = e^{j\frac{4\pi}{3}}$$

Matrix

$$\begin{pmatrix} \mathbf{U}_{ABC} \end{pmatrix} = \begin{pmatrix} \hat{\mathbf{U}}_A \\ \hat{\mathbf{U}}_B \\ \hat{\mathbf{U}}_C \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 \\ \hat{a}^2 & \hat{a} & 1 \\ \hat{a} & \hat{a}^2 & 1 \end{pmatrix} \begin{pmatrix} \hat{\mathbf{U}}_1 \\ \hat{\mathbf{U}}_2 \\ \hat{\mathbf{U}}_0 \end{pmatrix} = (\mathbf{T})(\mathbf{U}_{120})$$

Inversely

$$\begin{pmatrix} \mathbf{U}_{120} \end{pmatrix} = \begin{pmatrix} \hat{\mathbf{U}}_1 \\ \hat{\mathbf{U}}_2 \\ \hat{\mathbf{U}}_0 \end{pmatrix} = \frac{1}{3} \begin{pmatrix} 1 & \hat{a} & \hat{a}^2 \\ 1 & \hat{a}^2 & \hat{a} \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} \hat{\mathbf{U}}_A \\ \hat{\mathbf{U}}_B \\ \hat{\mathbf{U}}_C \end{pmatrix} = (\mathbf{T}^{-1})(\mathbf{U}_{ABC})$$

3ph power

$$\hat{S} = \hat{U}_A \hat{I}_A^* + \hat{U}_B \hat{I}_B^* + \hat{U}_C \hat{I}_C^* = \begin{pmatrix} \hat{U}_A & \hat{U}_B & \hat{U}_C \end{pmatrix} \begin{pmatrix} \hat{I}_A \\ \hat{I}_B \\ \hat{I}_C \end{pmatrix}^* = (\mathbf{U}_{ABC})^T (\mathbf{I}_{ABC})^*$$

$$\hat{S} = [(\mathbf{T})(\mathbf{U}_{120})]^T [(\mathbf{T})(\mathbf{I}_{120})]^* = (\mathbf{U}_{120})^T (\mathbf{T})^T (\mathbf{T})^* (\mathbf{I}_{120})^*$$

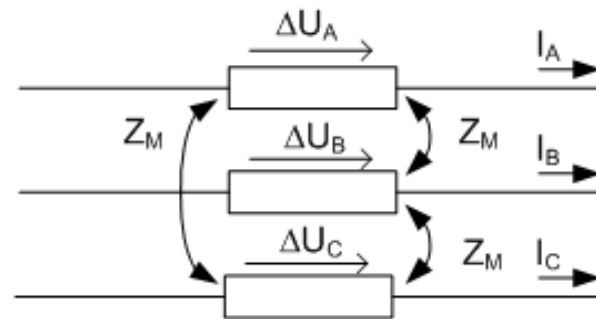
$$(\mathbf{T})^T (\mathbf{T})^* = \begin{pmatrix} 1 & \hat{a}^2 & \hat{a} \\ 1 & \hat{a} & \hat{a}^2 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 1 & 1 \\ \hat{a} & \hat{a}^2 & 1 \\ \hat{a}^2 & \hat{a} & 1 \end{pmatrix} = \begin{pmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{pmatrix} = 3(\mathbf{E})$$

$$\hat{S} = 3(\mathbf{U}_{120})^T (\mathbf{I}_{120})^*$$

$$\hat{S} = \underline{3(\hat{U}_1 \hat{I}_1^* + \hat{U}_2 \hat{I}_2^* + \hat{U}_0 \hat{I}_0^*)}$$

Series symmetrical segments in ES

$$\begin{pmatrix} \Delta \hat{U}_A \\ \Delta \hat{U}_B \\ \Delta \hat{U}_C \end{pmatrix} = \begin{pmatrix} \hat{Z} & \hat{Z}' & \hat{Z}' \\ \hat{Z}' & \hat{Z} & \hat{Z}' \\ \hat{Z}' & \hat{Z}' & \hat{Z} \end{pmatrix} \begin{pmatrix} \hat{I}_A \\ \hat{I}_B \\ \hat{I}_C \end{pmatrix}$$



$$(\Delta U_{ABC}) = (Z_{ABC})(I_{ABC})$$

$$(T)(\Delta U_{120}) = (Z_{ABC})(T)(I_{120})$$

$$(\Delta U_{120}) = (T)^{-1}(Z_{ABC})(T)(I_{120}) = (Z_{120})(I_{120})$$

$$\underline{(Z_{120}) = (T)^{-1}(Z_{ABC})(T)}$$

$$(Z_{120}) = \begin{pmatrix} \hat{Z}_1 & 0 & 0 \\ 0 & \hat{Z}_2 & 0 \\ 0 & 0 & \hat{Z}_0 \end{pmatrix} = \begin{pmatrix} \hat{Z} - \hat{Z}' & 0 & 0 \\ 0 & \hat{Z} - \hat{Z}' & 0 \\ 0 & 0 & \hat{Z} + 2\hat{Z}' \end{pmatrix}$$

Multiple lines

$$\begin{pmatrix} (\Delta U_{V1}) \\ (\Delta U_{V2}) \\ \dots \end{pmatrix}_{ABC} = (Z_{ABC}) \begin{pmatrix} (I_{V1}) \\ (I_{V2}) \\ \dots \end{pmatrix}_{ABC}$$

$$\begin{pmatrix} (T) & 0 & 0 \\ 0 & (T) & 0 \\ 0 & 0 & \dots \end{pmatrix} \begin{pmatrix} (\Delta U_{V1}) \\ (\Delta U_{V2}) \\ \dots \end{pmatrix}_{120} = (Z_{ABC}) \begin{pmatrix} (T) & 0 & 0 \\ 0 & (T) & 0 \\ 0 & 0 & \dots \end{pmatrix} \begin{pmatrix} (I_{V1}) \\ (I_{V2}) \\ \dots \end{pmatrix}_{120}$$

$$\begin{pmatrix} (\Delta U_{V1}) \\ (\Delta U_{V2}) \\ \dots \end{pmatrix}_{120} = \begin{pmatrix} (T) & 0 & 0 \\ 0 & (T) & 0 \\ 0 & 0 & \dots \end{pmatrix}^{-1} (Z_{ABC}) \begin{pmatrix} (T) & 0 & 0 \\ 0 & (T) & 0 \\ 0 & 0 & \dots \end{pmatrix} \begin{pmatrix} (I_{V1}) \\ (I_{V2}) \\ \dots \end{pmatrix}_{120}$$

$$\begin{pmatrix} (\Delta U_{V1}) \\ (\Delta U_{V2}) \\ \dots \end{pmatrix}_{120} = \begin{pmatrix} (T)^{-1} & 0 & 0 \\ 0 & (T)^{-1} & 0 \\ 0 & 0 & \dots \end{pmatrix} (Z_{ABC}) \begin{pmatrix} (T) & 0 & 0 \\ 0 & (T) & 0 \\ 0 & 0 & \dots \end{pmatrix} \begin{pmatrix} (I_{V1}) \\ (I_{V2}) \\ \dots \end{pmatrix}_{120}$$

Shunt symmetrical segments in ES

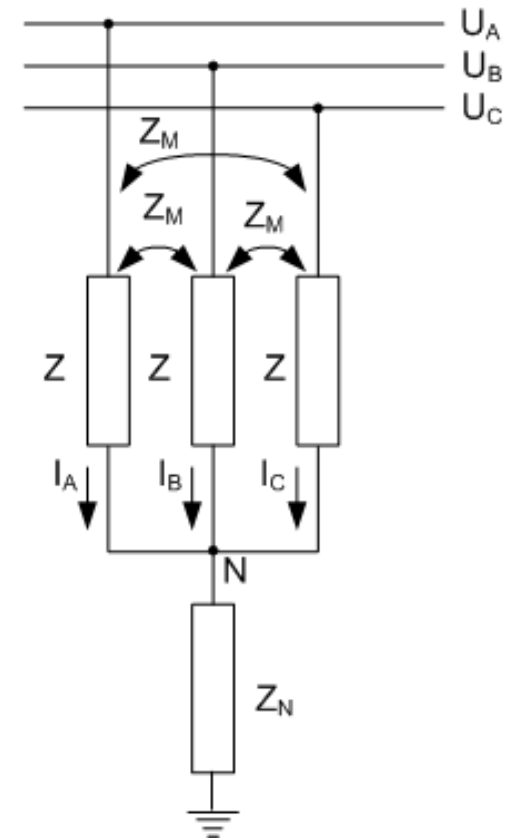
$$\begin{pmatrix} U_{ABC} \end{pmatrix} = \begin{pmatrix} Z_{ABC} \end{pmatrix} \begin{pmatrix} I_{ABC} \end{pmatrix} + \begin{pmatrix} Z_N \end{pmatrix} \begin{pmatrix} I_{ABC} \end{pmatrix}$$

$$\begin{pmatrix} Z_N \end{pmatrix} = \begin{pmatrix} \hat{Z}_N & \hat{Z}_N & \hat{Z}_N \\ \hat{Z}_N & \hat{Z}_N & \hat{Z}_N \\ \hat{Z}_N & \hat{Z}_N & \hat{Z}_N \end{pmatrix}$$

$$\begin{pmatrix} U_{120} \end{pmatrix} = \begin{pmatrix} T \end{pmatrix}^{-1} \begin{pmatrix} Z_{ABC} \end{pmatrix} \begin{pmatrix} T \end{pmatrix} \begin{pmatrix} I_{120} \end{pmatrix} + \begin{pmatrix} T \end{pmatrix}^{-1} \begin{pmatrix} Z_N \end{pmatrix} \begin{pmatrix} T \end{pmatrix} \begin{pmatrix} I_{120} \end{pmatrix}$$

$$\begin{pmatrix} Z_{120} \end{pmatrix} = \begin{pmatrix} T \end{pmatrix}^{-1} \left[\begin{pmatrix} Z_{ABC} \end{pmatrix} + \begin{pmatrix} Z_N \end{pmatrix} \right] \begin{pmatrix} T \end{pmatrix}$$

$$\begin{pmatrix} Z_{120} \end{pmatrix} = \begin{pmatrix} \hat{Z} - \hat{Z}' & 0 & 0 \\ 0 & \hat{Z} - \hat{Z}' & 0 \\ 0 & 0 & \hat{Z} + 2\hat{Z}' + 3Z_N \end{pmatrix}$$



Symmetrical components voltages in the symmetrical segments depend only on the corresponding component current and component impedance.

Inductors and capacitors in ES

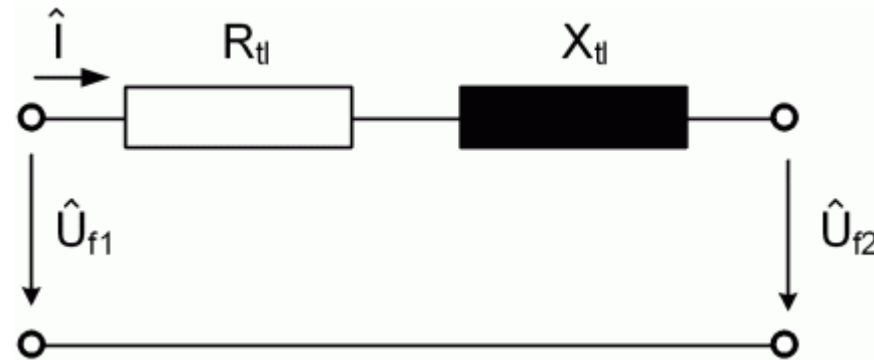
a) Series inductors

- reactors are used to limit short-circuit currents
- used in grids up to 35 kV, single-phase ($I_n > 200\text{A}$) or three-phase ($I_n < 200\text{A}$), usually air-cooled (small L)
- the same design in LC filters for harmonics suppression





$$R_{tl} \ll X_{tl}$$



Input: $X_{tl\%}$, S_{tl} , U_n , I_n

Calculation: $S_{tl} = \sqrt{3} \cdot U_n \cdot I_n$

$$X_{tl} = \frac{X_{t\%} \cdot U_n}{100 \cdot \sqrt{3} \cdot I_n} = \frac{X_{t\%} \cdot U_n^2}{100 \cdot S_{tl}}$$

$$\Delta \hat{U}_f = \hat{U}_{f1} - \hat{U}_{f2} = (R_t + jX_t) \hat{I} = \hat{Z}_t \hat{I}$$

$$\begin{bmatrix} \hat{Z}_{tabc} \end{bmatrix} = \begin{bmatrix} \hat{Z}_{t012} \end{bmatrix} = \hat{Z}_t \cdot [E] - \text{3ph inductor}$$

→ self-impedance \hat{Z}_t , mutual impedances 0

In fault-free state the inductor can be bypassed by a fuse to reduce a voltage drop.

b) Shunt (parallel) inductors

- in the systems $U_N > 220$ kV, oil cooling, Fe core
- used to compensate capacitive (charging) currents of overhead lines for no-load or small loads \rightarrow U control:

$$X_{tl} = \frac{U_{tl n}}{\sqrt{3} \cdot I_{tl n}} = \frac{U_{tl n}^2}{Q_{tl n}}$$

$$\hat{Z}_{tl} = \hat{Z}_{tl1} = \hat{Z}_{t2}, Z_{tl0} \rightarrow \infty$$

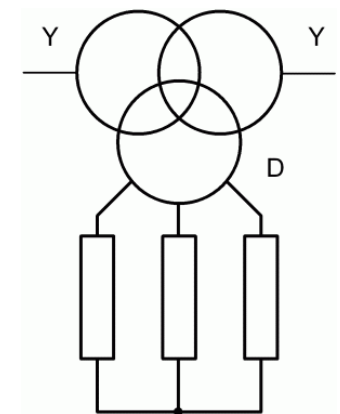
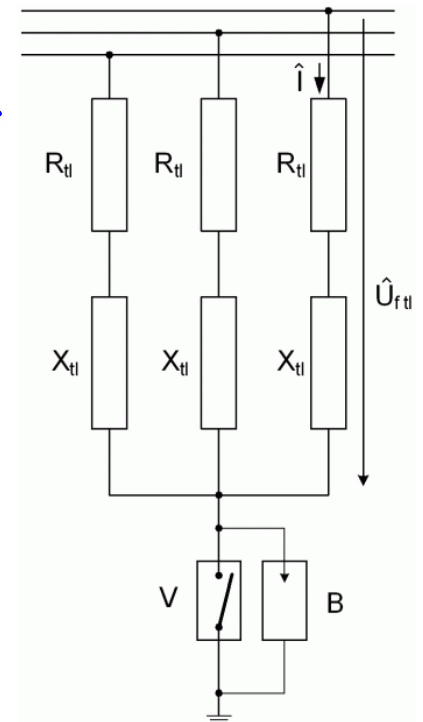
Connection in the system:

a) galvanic connection to the line

- Y winding, neutral point connected to the ground through V only during auto-reclosing (disturbances)

b) inductor connection to transformer tertiary winding

- lower voltage $U_n \approx 10 \div 35$ kV
- problem with switch-off (purely inductive load)

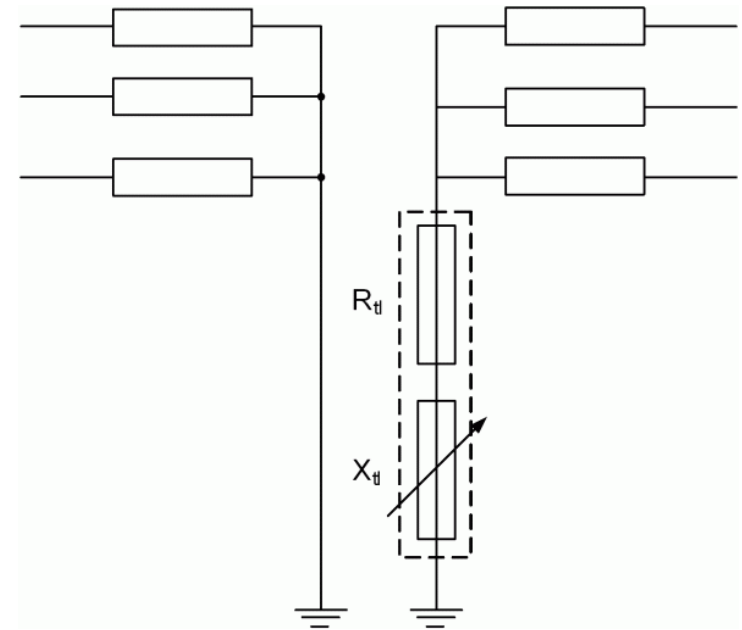


Kočín 400 kV



c) Neutral point inductors

- used in networks with indirectly earthed neutral point to compensate currents during ground fault
- value of the fault current does not depend on the ground fault position and the current is capacitive
- inductor reactance X_{tl} should assure that the value of the inductive current is equal to the value of capacitive current \rightarrow arc extinction
- for voltage 6 to 35 kV (rated at U_{fn}), reactor is single-phased!, oil cooling
- capacitive current change (network reconfiguration) \rightarrow change in inductance (air gap correction in the magnetic circuit)
= arc-suppression coil (Peterson coil)
- it doesn't occur in positive and negative sequence component, $X_0 = 3X_{tl}$

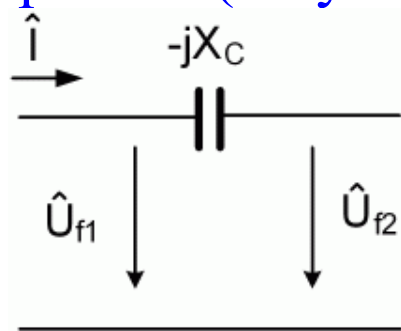


6 MVar, 13 kV, Sokolnice

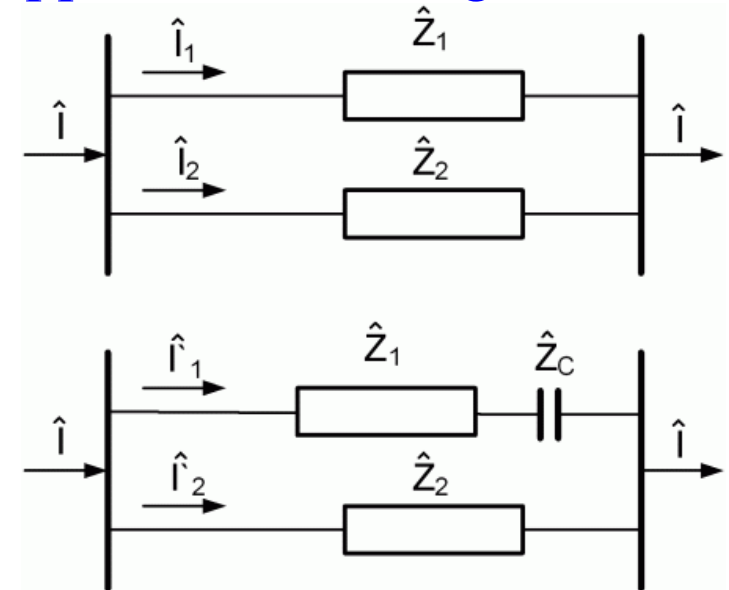


d) Series capacitors

- capacitors in ES = capacitor banks = series and parallel connection
- to improve voltage conditions (MV lines) or adjusting parameters (long HV lines)
- voltage and power of the capacitor varies with the load
- during short-circuits and overcurrents there appears overvoltage on the capacitor (very fast protections are used)



$$\hat{U}_C = -j \frac{1}{\omega C} \hat{I}$$



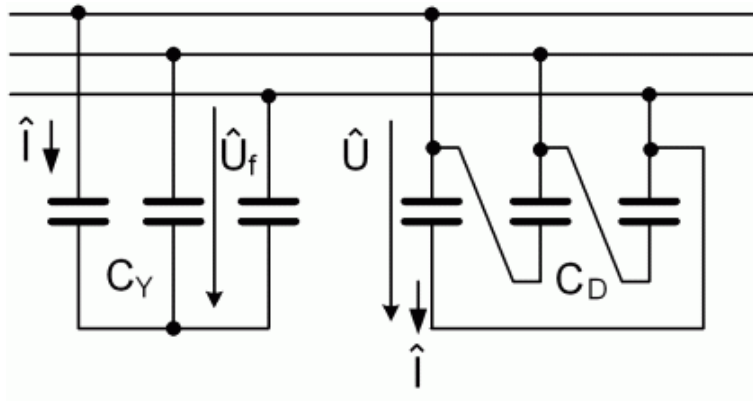
- C must be insulated against the ground (insulated platforms) – C under voltage
- drawback – allows harmonic currents flow
- current distribution among parallel transmission lines could be achieved

Canada 750 kV



e) Shunt capacitors

- used in industrial networks up to 1 kV
- connection:
 - a) wye - Y
 - b) delta - Δ (D)



$$Q_f = U_f \cdot I_C = U_f^2 \omega C_Y \quad Q_f = U \cdot I_C = U^2 \omega C_\Delta$$
$$Q = 3U_f^2 \omega C_Y = U^2 \omega C_Y \quad Q = 3U^2 \omega C_\Delta$$

- with the same reactive power

$$U^2 \omega C_Y = 3U^2 \omega C_\Delta \rightarrow C_Y = 3C_\Delta \rightarrow \text{rather delta}$$



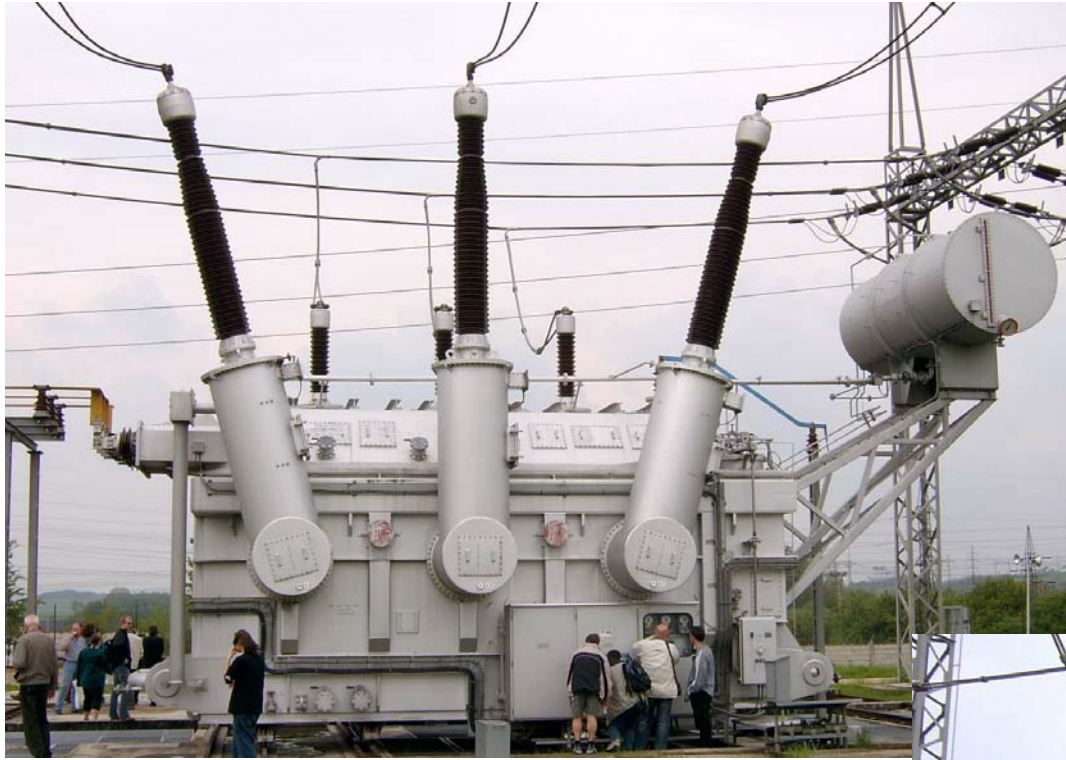
- reactive power compensation
 - a) $Q_C < Q$ under-compensated
 - b) $Q_C = Q$ exact compensation
 - c) $Q_C > Q$ over-compensated

→ power factor improvement, lower power losses, voltage drops

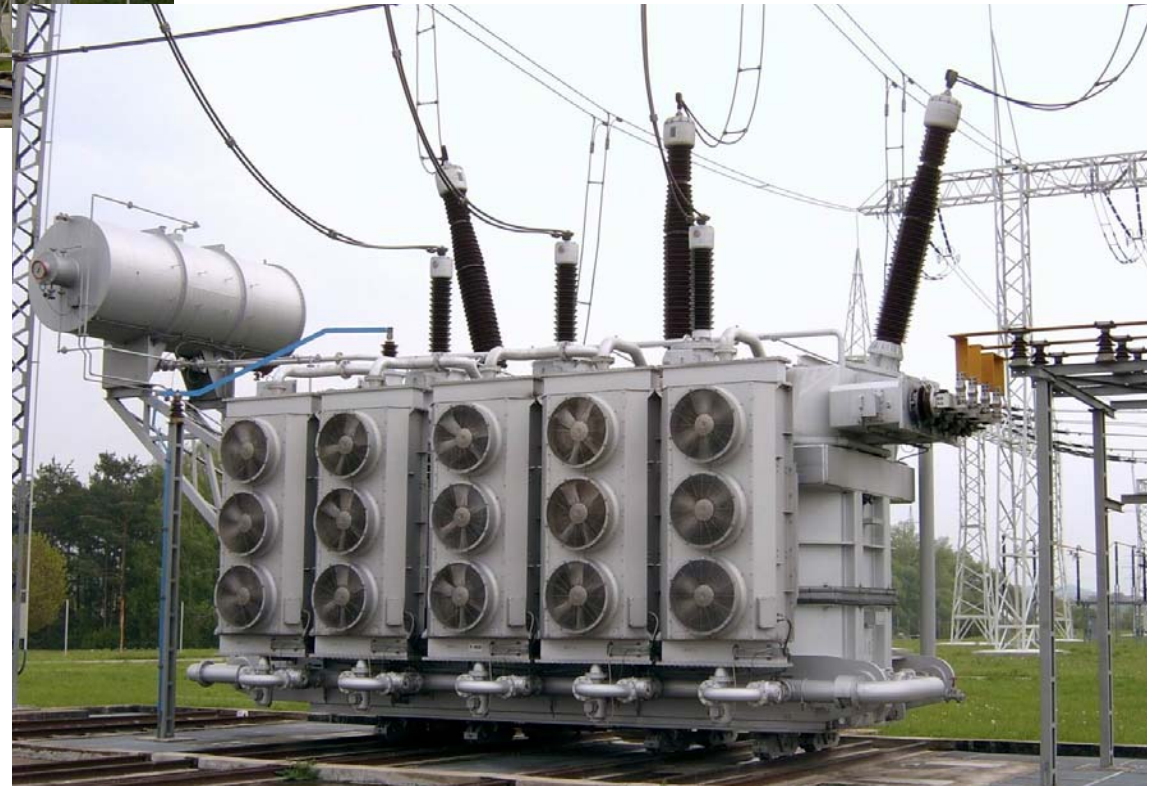
- individual or group compensation could be used

Transformer parameters





350 MVA, 400/110 kV
YNauto - d1, Sokolnice



a) Two-winding transformers

- winding connection Y, Yn, D, Z, Zn, V

Yzn – distribution TRF MV/LV up to 250 kVA, for unbalanced load

Dyn – distribution TRF MV/LV from 400 kVA

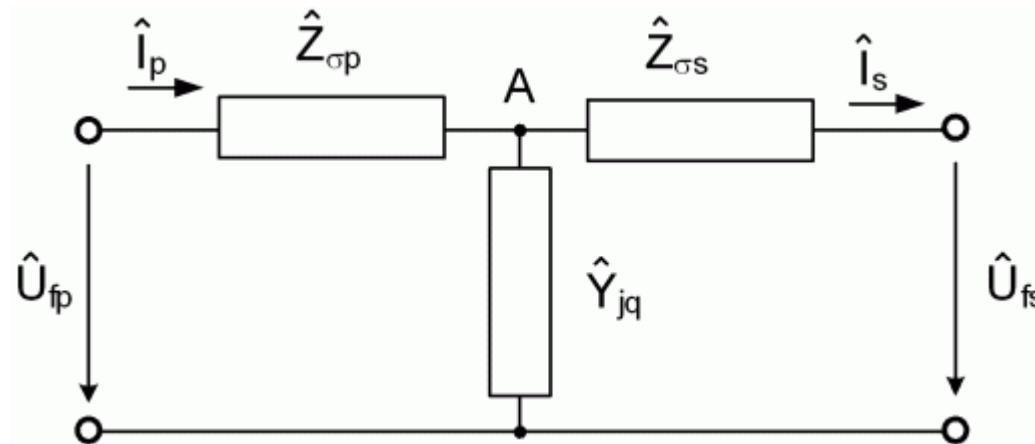
Yd – block TRF in power plants, the 3rd harmonic suppression

Yna-d, YNynd – power grid transformer (400, 220, 110 kV)

YNyd – power grid transformer (e.g. 110/23/6,3 kV)

- equivalent circuit: T – network

$$\hat{Z}_{\sigma p} = R_p + jX_{\sigma p} \quad \hat{Z}_{\sigma s} = R_s + jX_{\sigma s} \quad \hat{Y}_{jq} = G_q - jB_q$$



- each phase can be considered separately (unbalance is neglected), i.e. operational impedance (positive sequence) is used
- values of the parameters are calculated, then verified by no-load and short-circuit tests
 - o *no-load test* – secondary winding open, primary w. supplied by rated voltage, no-load current flows (lower than rated one)
 - o *short-circuit test* – secondary winding short-circuit, primary w. supplied by short-circuit voltage (lower than rated one) so that rated current flows

ΔP_0 (W), i_0 (%), ΔP_k (W), $z_k = u_k$ (%), S_n (VA), U_n (V)

$u_k \approx 4 \div 14$ % (increases with TRF power)

$p_k \approx 0,1 \div 1$ % (decreases with TRF power)

$p_0 \approx 0,01 \div 0,1$ % (decreases with TRF power)

- shunt branch:

$$g_q = \frac{\Delta P_0}{S_n} \quad y_q = \frac{i_{0\%}}{100} \quad b_q = \sqrt{y_q^2 - g_q^2}$$

$$\hat{y}_q = \frac{\Delta P_0}{S_n} - j \sqrt{\left(\frac{i_{0\%}}{100}\right)^2 - \left(\frac{\Delta P_0}{S_n}\right)^2} = g_q - j \cdot b_q$$

$$\hat{Y}_q = \hat{y}_q \frac{S_n}{U_n^2} = \frac{S_n}{U_n^2} \left[\frac{\Delta P_0}{S_n} - j \sqrt{\left(\frac{i_{0\%}}{100}\right)^2 - \left(\frac{\Delta P_0}{S_n}\right)^2} \right] = G_q - j \cdot B_q$$

- series branch:

$$r_k = \frac{\Delta P_k}{S_n} \quad z_k = \frac{u_{k\%}}{100} \quad x_k = \sqrt{z_k^2 - r_k^2}$$

$$\hat{z}_k = \frac{\Delta P_k}{S_n} + j \sqrt{\left(\frac{u_{k\%}}{100}\right)^2 - \left(\frac{\Delta P_k}{S_n}\right)^2} = r_k + j \cdot x_k$$

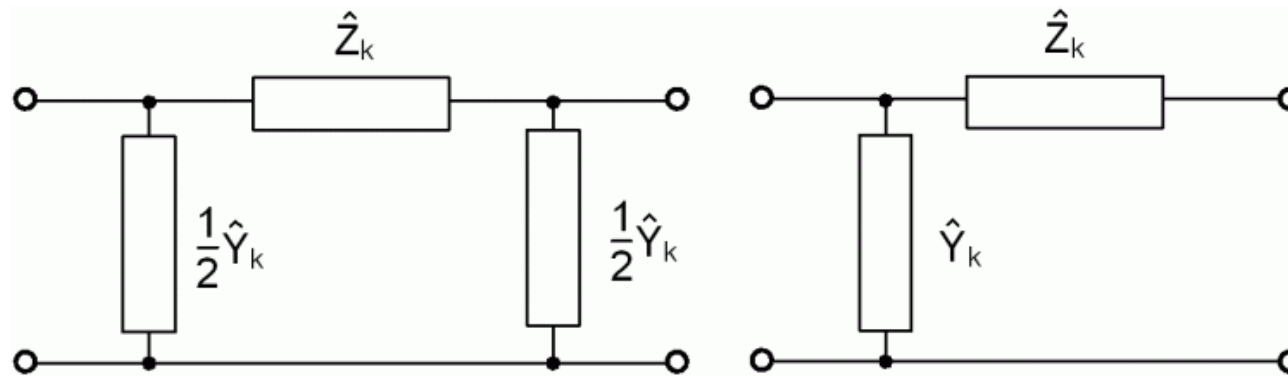
$$\hat{Z}_k = \hat{z}_k \frac{U_n^2}{S_n} = \frac{U_n^2}{S_n} \left[\frac{\Delta P_k}{S_n} + j \sqrt{\left(\frac{u_{k\%}}{100}\right)^2 - \left(\frac{\Delta P_k}{S_n}\right)^2} \right] = R_k + j \cdot X_k$$

$$\hat{Z}_{\sigma ps} = \hat{Z}_k = (R_p + R_s) + j(X_{\sigma p} + X_{\sigma s})$$

- we choose $\hat{Z}_{\sigma p} = 0,5\hat{Z}_{\sigma ps} = \hat{Z}_{\sigma s}$

- this division is not physically correct (different leakage flows, different resistances)

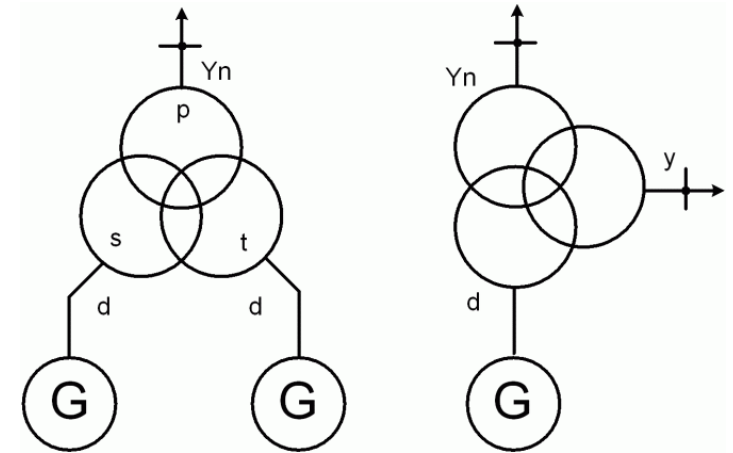
- usage of T-network to calculate meshed systems is not appropriate sometimes (it adds another node)
- therefore calculation using π -network, Γ -network



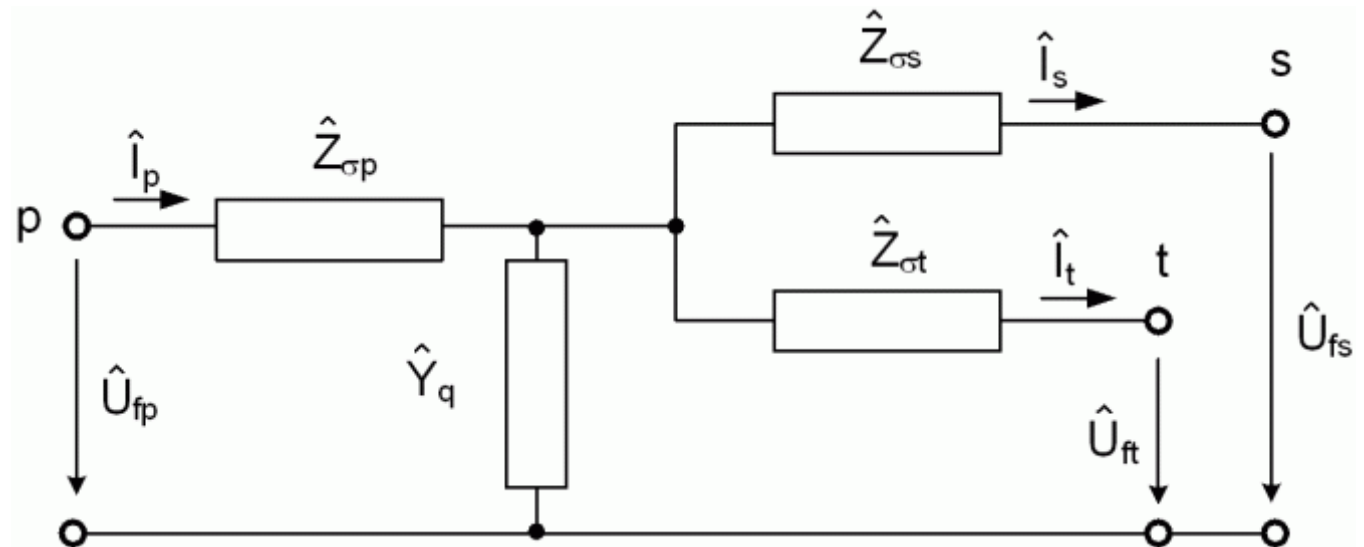
b) Three-winding transformers

- parameters are calculated, then verified by no-load and short-circuit measurements (3 short-circuit tests: 1 winding no-load, 1 short-circuit and 1 supplied):

ΔP_0 (W), i_0 (%), ΔP_k (W), $z_K = u_K$ (%),
 S_n (VA), U_n (V)



- powers needn't be the same: e.g. $S_{Sn} = S_{Tn} = 0,5 \cdot S_{Pn}$
- equivalent circuit:



- no-load measurement:

related to the primary rated power and rated voltage S_{Pn} a U_{Pn} (supplied)

$$\hat{y}_q = g_q - j \cdot b_q = \frac{\Delta P_0}{S_{Pn}} - j \sqrt{\left(\frac{i_{0\%}}{100}\right)^2 - \left(\frac{\Delta P_0}{S_{Pn}}\right)^2}$$

denominated value (S) – related to U_{Pn}

$$\hat{Y}_q = \hat{y}_q \frac{S_{Pn}}{U_{Pn}^2} = G_q - j \cdot B_q = \frac{S_{Pn}}{U_{Pn}^2} \left[\frac{\Delta P_0}{S_{Pn}} - j \sqrt{\left(\frac{i_{0\%}}{100}\right)^2 - \left(\frac{\Delta P_0}{S_{Pn}}\right)^2} \right]$$

- short-circuit measurement: (3x, supply – short-circuit – no-load)

provided: $S_{Pn} \neq S_{Sn} \neq S_{Tn}$

measurement between	P - S	P - T	S - T
short-circuit losses (W)	ΔP_{kPS}	ΔP_{kPT}	ΔP_{kST}
short-circuit voltage (%)	u_{kPS}	u_{kPT}	u_{kST}
measurement corresponds to power (VA)	S_{Sn}	S_{Tn}	S_{Tn}

short-circuit tests S – T:

parameter to be found:

$$\hat{Z}_{ST} = \hat{Z}_{\sigma S} + \hat{Z}_{\sigma T} \left(\hat{Z}_{\sigma S} = R_S + j \cdot X_{\sigma S} \right) - \text{recalculated to } U_{Pn}$$

$$\hat{Z}_{ST} = \hat{Z}_{\sigma S} + \hat{Z}_{\sigma T} - \text{recalculated to } U_{Pn}, S_{Pn}$$

$$\Delta P_k \text{ for } I_{Tn} \rightarrow \Delta P_{kST} = 3 \cdot R_{ST}^+ \cdot I_{Tn}^2, \quad I_{Tn} = \frac{S_{Tn}}{\sqrt{3} \cdot U_{Tn}}$$

R_{ST}^+resistance of secondary and tertiary windings (related to U_{Tn})

$$R_{ST}^+ = \frac{\Delta P_{kST}}{S_{Tn}^2} \cdot U_{Tn}^2$$

$$R_{ST} = R_{ST}^+ \cdot \frac{U_{Pn}^2}{U_{Tn}^2} \rightarrow R_{ST} = R_S + R_T = \frac{\Delta P_{kST}}{S_{Tn}^2} \cdot U_{Pn}^2$$

r_S (r_T)...resistance of sec. and ter. windings recalculated to primary

$$r_{ST} = R_{ST} \cdot \frac{S_{Pn}}{U_{Pn}^2} = \frac{\Delta P_{kST}}{S_{Tn}^2} \cdot S_{Pn}$$

- impedance:

$$Z_{ST} = \frac{u_{kST\%}}{100} \cdot \frac{S_{Pn}}{S_{Tn}}, \quad Z_{ST} = z_{ST} \cdot \frac{U_{Pn}^2}{S_{Pn}} = \frac{u_{kST\%}}{100} \cdot \frac{U_{Pn}^2}{S_{Tn}}$$

$$\hat{Z}_{ST} = r_{ST} + j \cdot X_{ST}, \quad X_{ST} = \sqrt{Z_{ST}^2 - r_{ST}^2}, \quad X_{ST} = X_{\sigma S} + X_{\sigma T}$$

- based on the derived relations we can write:

P - S:

$$\hat{Z}_{PS} = r_{PS} + j \cdot X_{PS} = \frac{\Delta P_{kPS}}{S_{Sn}^2} \cdot S_{Pn} + j \cdot \sqrt{\left(\frac{u_{kPS\%}}{100} \cdot \frac{S_{Pn}}{S_{Sn}} \right)^2 - \left(\frac{\Delta P_{kPS}}{S_{Sn}^2} \cdot S_{Pn} \right)^2}$$

$$\hat{Z}_{PS} = R_{PS} + j \cdot X_{PS} = \frac{\Delta P_{kPS}}{S_{Sn}^2} \cdot U_{Pn}^2 + j \cdot \sqrt{\left(\frac{u_{kPS\%}}{100} \cdot \frac{U_{Pn}^2}{S_{Sn}} \right)^2 - \left(\frac{\Delta P_{kPS}}{S_{Sn}^2} \cdot U_{Pn}^2 \right)^2}$$

- analogous for P – T and S – T

- leakage reactances for P, S, T:

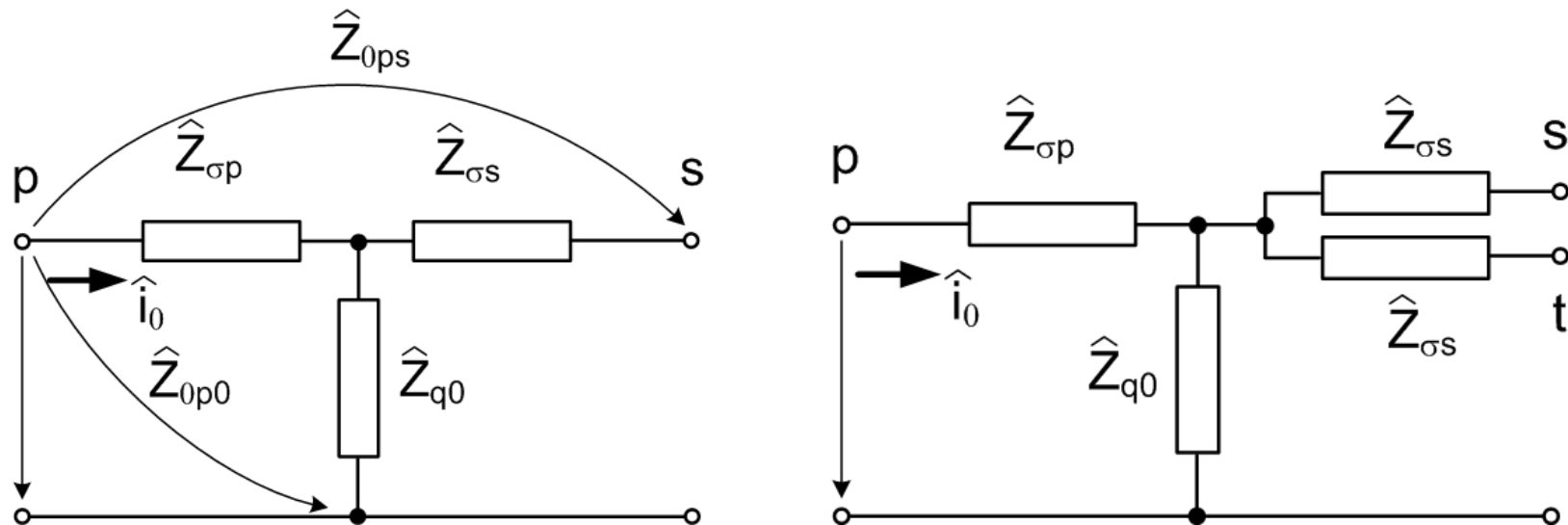
$$\hat{Z}_{\sigma P} = R_P + j \cdot X_{\sigma P} = 0,5 \cdot (\hat{Z}_{PS} + \hat{Z}_{PT} - \hat{Z}_{ST})$$

$$\hat{Z}_{\sigma S} = R_S + j \cdot X_{\sigma S} = 0,5 \cdot (\hat{Z}_{PS} + \hat{Z}_{ST} - \hat{Z}_{PT})$$

$$\hat{Z}_{\sigma T} = R_T + j \cdot X_{\sigma T} = 0,5 \cdot (\hat{Z}_{PT} + \hat{Z}_{ST} - \hat{Z}_{PS})$$

- knowledge of the series impedances and shunt admittances allows to study voltage and power conditions of 3-winding transformers
- mentioned impedances are valid for positive and negative sequences

Transformers zero sequence impedances



Series parameters are the same as for the positive sequence, the shunt always need to be determined.

Assumptions:

- Zero sequence voltage supplies the primary winding.
- The relative values are related to U_{Pn} and S_{Pn} .
- We distinguish free and tied magnetic flows (shell x core TRF).

Z_0 depends on the winding connection.

note: reluctance, inductance

magnetic resistance (reluctance)

$$R_m = \frac{1}{\mu} \frac{l}{S} \quad \text{analogy} \quad R_e = \frac{1}{\gamma} \frac{l}{S} = \rho \frac{l}{S}$$

magnetic flux (Hopkinson's law)

$$\Phi = \frac{N \cdot I}{R_m} \quad \text{analogy (Ohm's law)} \quad I = \frac{U}{R_e}$$

$$L = \frac{\Phi_c}{I} = \frac{N \cdot \Phi}{I} = \frac{N^2}{R_m}$$

$$\mu_{Fe} \gg \mu_0 \Rightarrow R_{mFe} \ll R_{m0} \Rightarrow L_{Fe} \gg L_{\sigma}$$

TRF magnetic circuit

$$\Phi = \Phi_h + \Phi_{\sigma} = \frac{N \cdot I}{R_{mFe}} + \frac{N \cdot I}{R_{m0}} = \frac{L_{Fe} \cdot I}{N} + \frac{L_{\sigma} \cdot I}{N} = \frac{I}{N} (L_{Fe} + L_{\sigma})$$

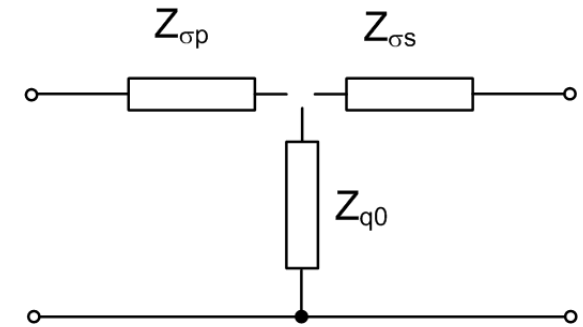
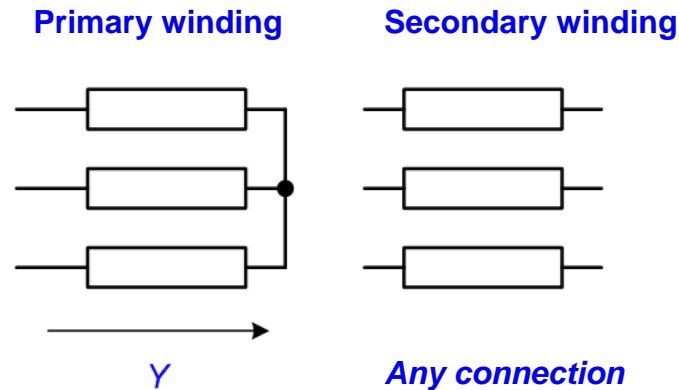
a) Y / any connection

$$3i_0 = 0$$

$$Z_0 = \frac{u_0}{i_0} \rightarrow \infty$$

$$Z_{0p0} \rightarrow \infty$$

$$Z_{0ps} \rightarrow \infty$$



b) D / any connection

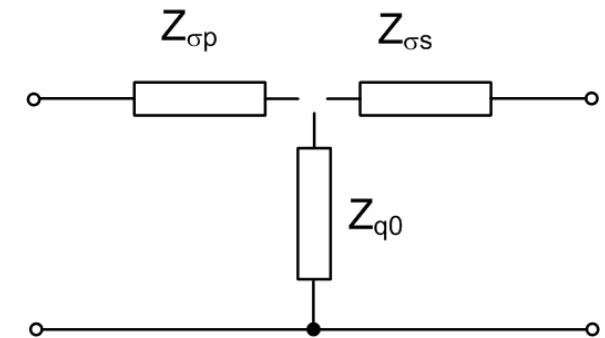
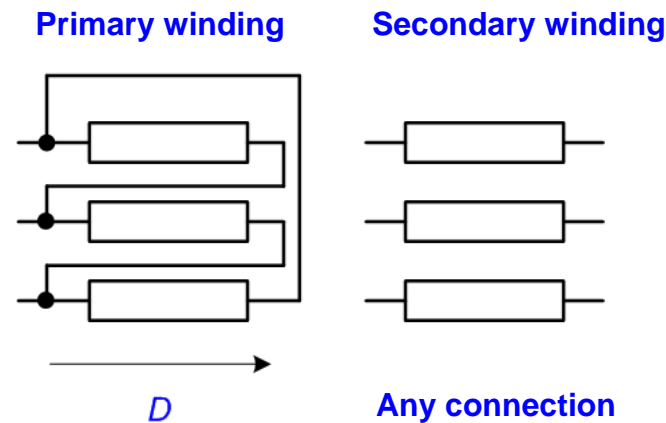
Zero sequence voltage is attached to D \rightarrow voltage at each phase

$$u_0 - u_0 = 0 \rightarrow i_a = i_b = i_c = 0 \rightarrow i_0 = 0$$

$$Z_0 = \frac{u_0}{i_0} \rightarrow \infty$$

$$Z_{0p0} \rightarrow \infty$$

$$Z_{0ps} \rightarrow \infty$$



c) **YN / D**

Currents in the primary winding i_0 induce currents i_0' in the secondary winding to achieve magnetic balance.

Currents i_0' in the secondary winding are short-closed and do not flow further into the grid.

$$\hat{Z}_{0p0} = \hat{Z}_{\sigma p} + \hat{Z}_{q0}$$

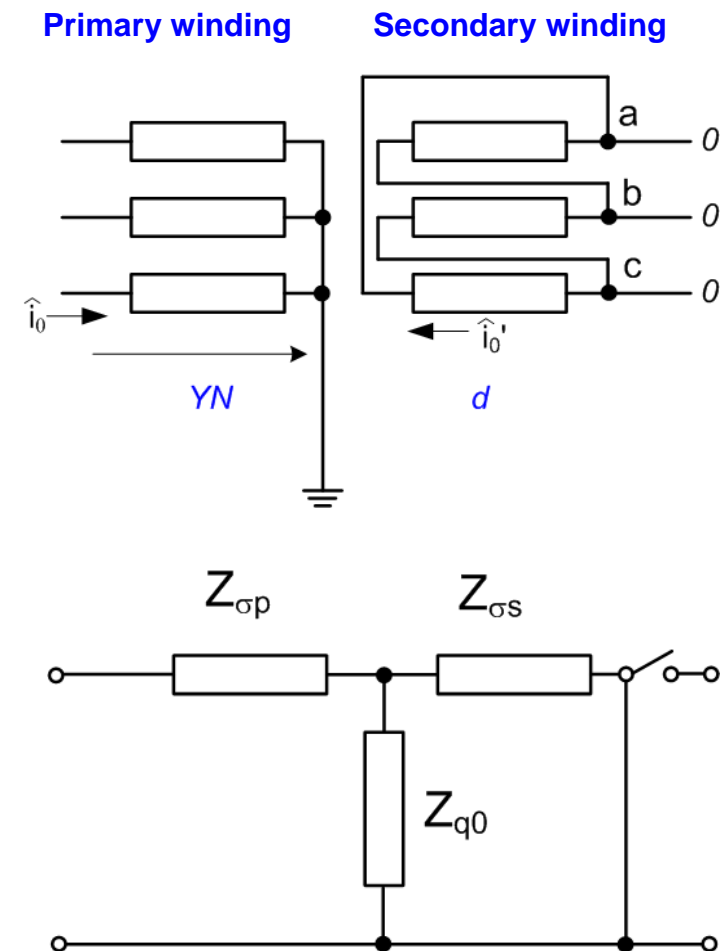
$$\hat{Z}_0 = \frac{\hat{u}_0}{\hat{i}_0} = \hat{Z}_{\sigma p} + \frac{\hat{Z}_{\sigma s} \cdot \hat{Z}_{q0}}{\hat{Z}_{\sigma s} + \hat{Z}_{q0}}$$

shell

$$\hat{Z}_{q0} = \hat{y}_q^{-1} \gg \hat{Z}_{\sigma s} \rightarrow \hat{Z}_0 \approx \hat{Z}_{\sigma ps} = \hat{Z}_{1k}$$

3-core

$$|\hat{Z}_{q0}| < |\hat{y}_q^{-1}| \rightarrow |\hat{Z}_0| \approx (0,7 \div 0,9) |\hat{Z}_{\sigma ps}|$$



d) YN / Y

Zero sequence current can't flow through the secondary winding.
Current i_0 corresponds to the magnetization current.

$$Z_{0ps} \rightarrow \infty$$

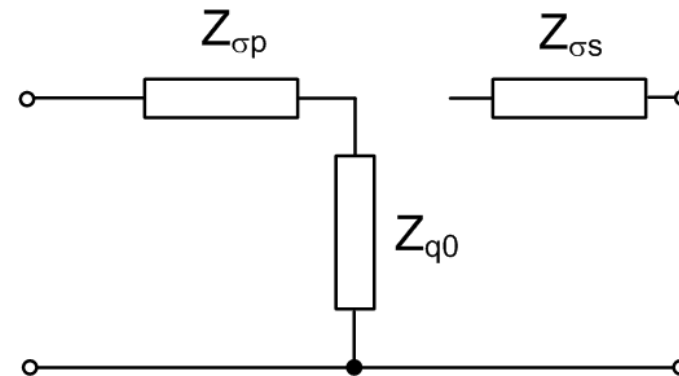
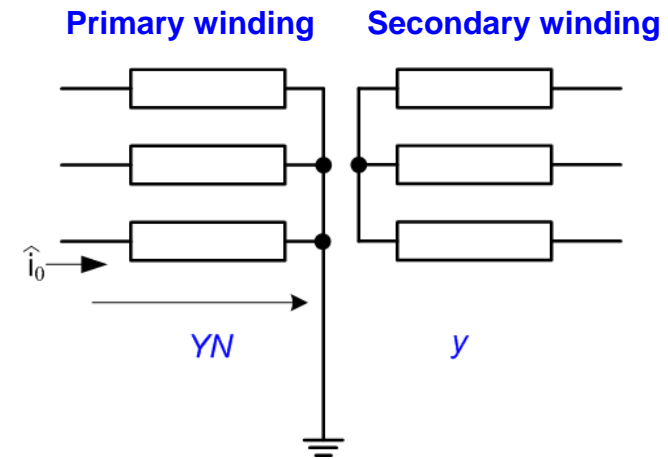
$$\hat{Z}_0 = \hat{Z}_{0p0} = \hat{Z}_{\sigma p} + \hat{Z}_{q0}$$

shell

$$\hat{Z}_{q0} = \hat{y}_q^{-1} \rightarrow Z_0 \rightarrow \infty$$

3-core

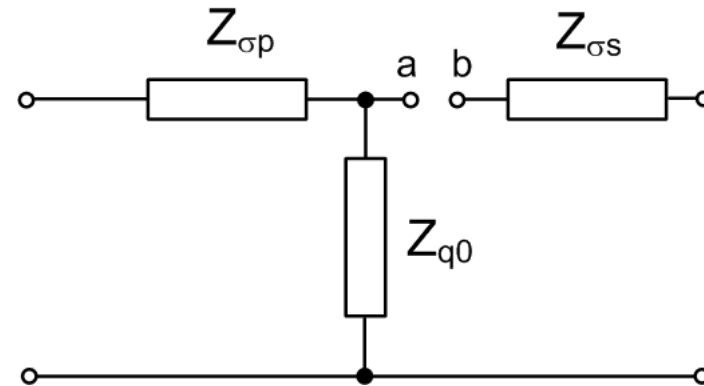
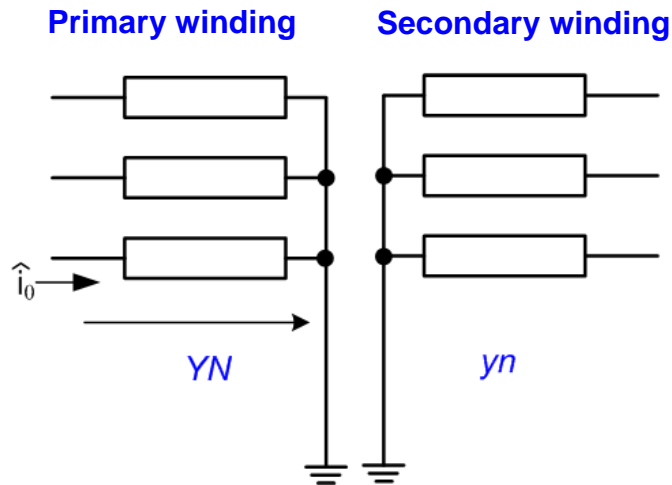
$$|\hat{Z}_{q0}| < |\hat{y}_q^{-1}| \rightarrow |\hat{Z}_0| \approx (0,3 \div 1)$$



e) **YN / YN**

If element with YN or ZN behind TRF \rightarrow points a-b are connected \rightarrow as the positive sequence.

If element with Y, Z or D behind TRF \rightarrow a-b are disconnected \rightarrow as YN / Y.



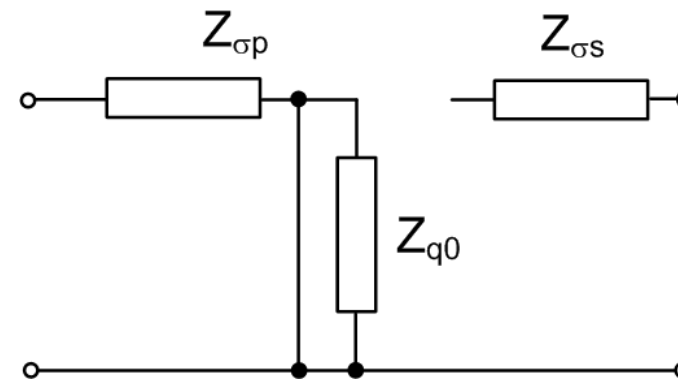
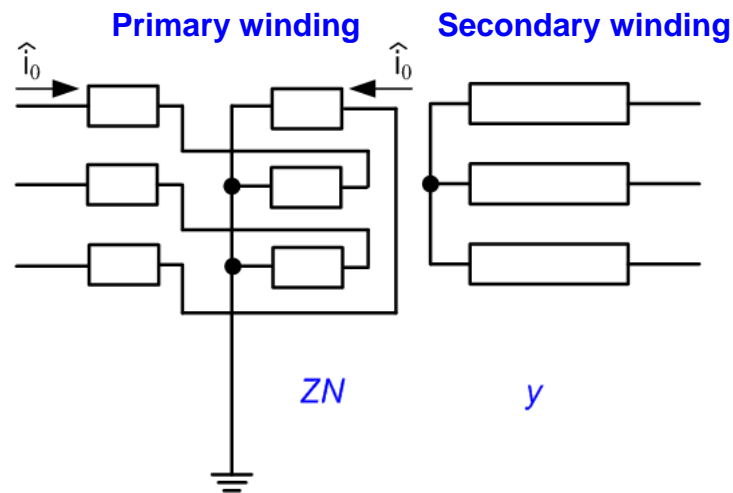
f) ZN / any connection

Currents i_0 induce mag. balance on the core themselves \rightarrow only leakages between the halves of the windings.

$$Z_{0ps} \rightarrow \infty$$

$$\hat{Z}_0 = \hat{Z}_{0p0} \approx (0,1 \div 0,3) \hat{Z}_{\sigma ps}$$

$$r_0 = r_p$$



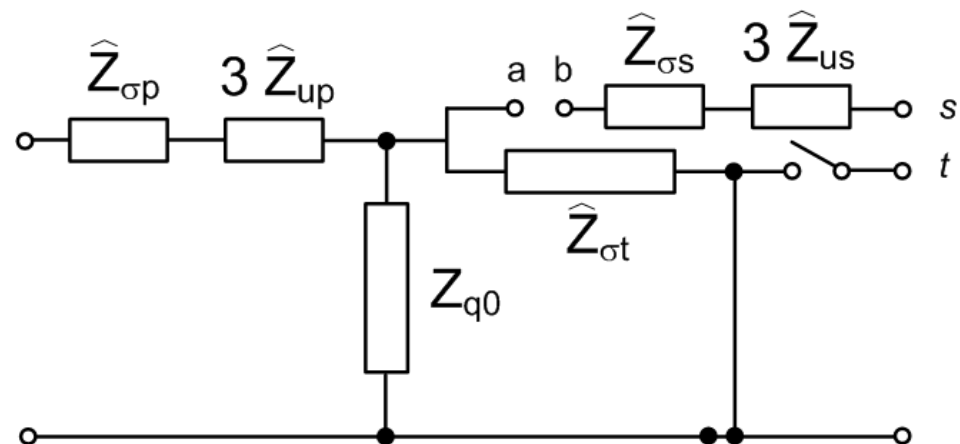
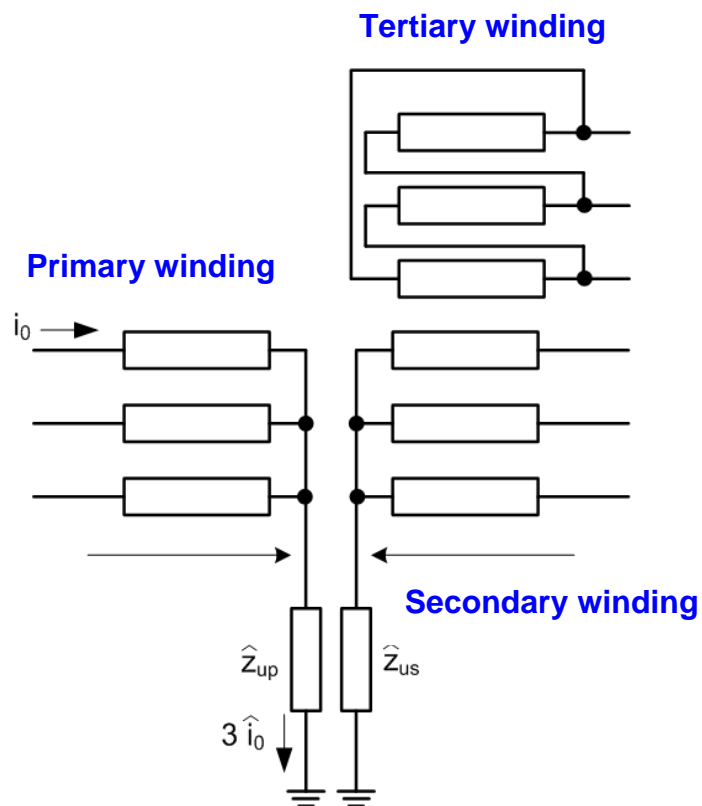
g) impedance in the neutral point

Current flowing through the neutral point is $3i_0$.

Voltage drop:
$$\Delta \hat{u}_{uz} = \hat{Z}_u \cdot 3\hat{i}_0 = 3\hat{Z}_u \cdot \hat{i}_0$$

→ in the model $3\hat{Z}_u$ in series with the leakage reactance

h) three-winding TRF



System equivalent

Impedance (positive sequence) is given by the nominal voltage and short-circuit current (power).

Three-phase (symmetrical) short-circuit: S_k'' (MVA), I_k'' (kA)

$$S_k'' = \sqrt{3} U_n I_k''$$

$$Z_s = \frac{U_n^2}{S_k''} = \frac{U_n}{\sqrt{3} \cdot I_k''}$$

CR:	400 kV	$S_k'' \approx (6000 \div 30000) \text{ MVA}$	$I_k'' \approx (9 \div 45) \text{ kA}$
	220 kV	$S_k'' \approx (2000 \div 12000) \text{ MVA}$	$I_k'' \approx (2 \div 30) \text{ kA}$
	110 kV	$S_k'' \approx (100x \div 3000) \text{ MVA}$	$I_k'' \approx (x \div 15) \text{ kA}$