

Simple transmission stability

Interconnected systems operate in synchronous operation (same frequency) if active power is less than limit value. Otherwise, system gets out of synchronism (parallel operation stability disturbance)

Steady-state stability – is the ability of the system to remain in the synchronous operation during small changes.

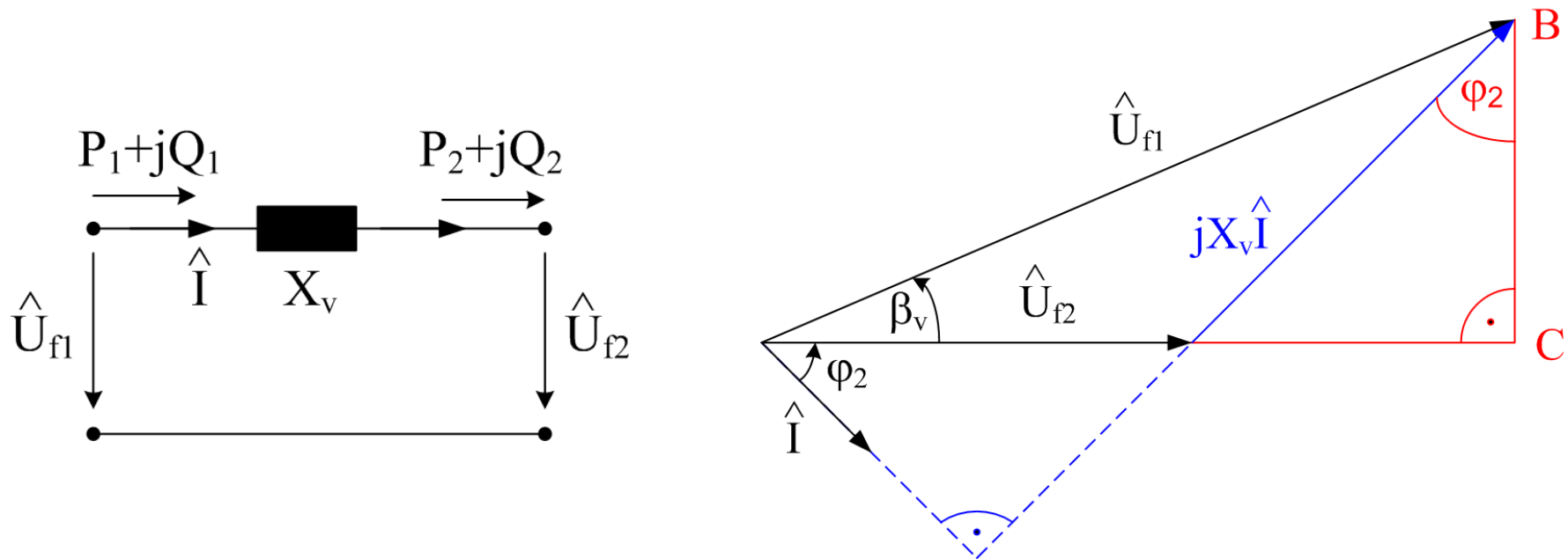
Transient stability – is the ability of the system to remain in the synchronous operation during sudden large changes (loading, parameters). Electromechanical transient events → need to have a sufficient power reserve during the steady-state operation.

Importance: sources and systems collaboration keeping, AC power lines length limiting

Basic relations

Assumption: only longitudinal reactance is considered

Transmission angle (power angle) β_v – between voltages at both transmission ends



Consumed active and reactive power (single phase)

$$P_f = U_{f2} I \cos \varphi_2$$

$$Q_f = U_{f2} I \sin \varphi_2$$

$$\overline{BC} \sim X_v I \cos \varphi_2 = U_{f1} \sin \beta_v$$

$$I \cos \varphi_2 = \frac{U_{f1}}{X_v} \sin \beta_v$$

Transmission power equation

$$P_f = \frac{U_{f1} U_{f2}}{X_v} \sin \beta_v$$

$0^\circ \div 90^\circ$: stable area

$90^\circ \div 180^\circ$: unstable area

$\beta_v = 90^\circ$: steady-state stability limit

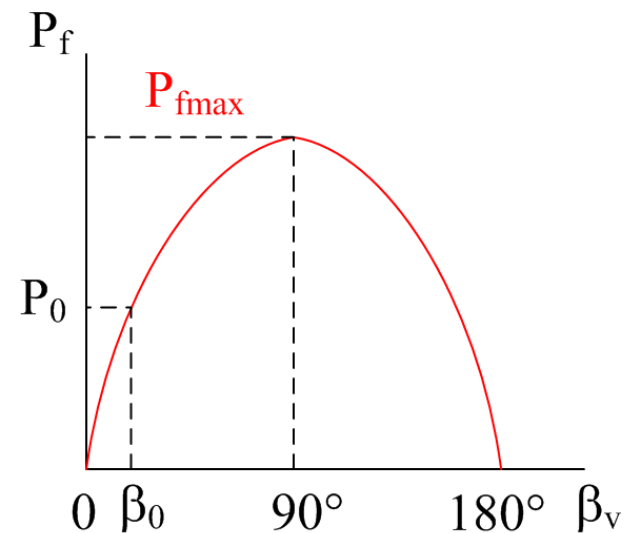
$$P_{f \max} = \frac{U_{f1} U_{f2}}{X_v}$$

In addition to power lines also reactance of generators, transformers ... are added → higher power angle. Generators have the biggest influence (X).

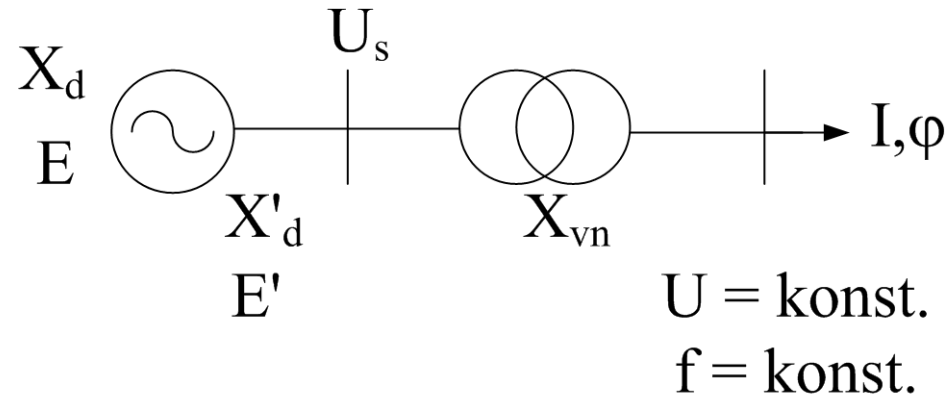
$$X_v I \sin \varphi_2 + U_{f2} = U_{f1} \cos \beta_v$$

$$I \sin \varphi_2 = \frac{U_{f1} \cos \beta_v}{X_v} - \frac{U_{f2}}{X_v}$$

$$Q_f = \frac{U_{f1} U_{f2} \cos \beta_v}{X_v} - \frac{U_{f2}^2}{X_v}$$



Turbo-alternator operating to a infinite power system



$$X_{dc} = X_d + X_{vn}$$

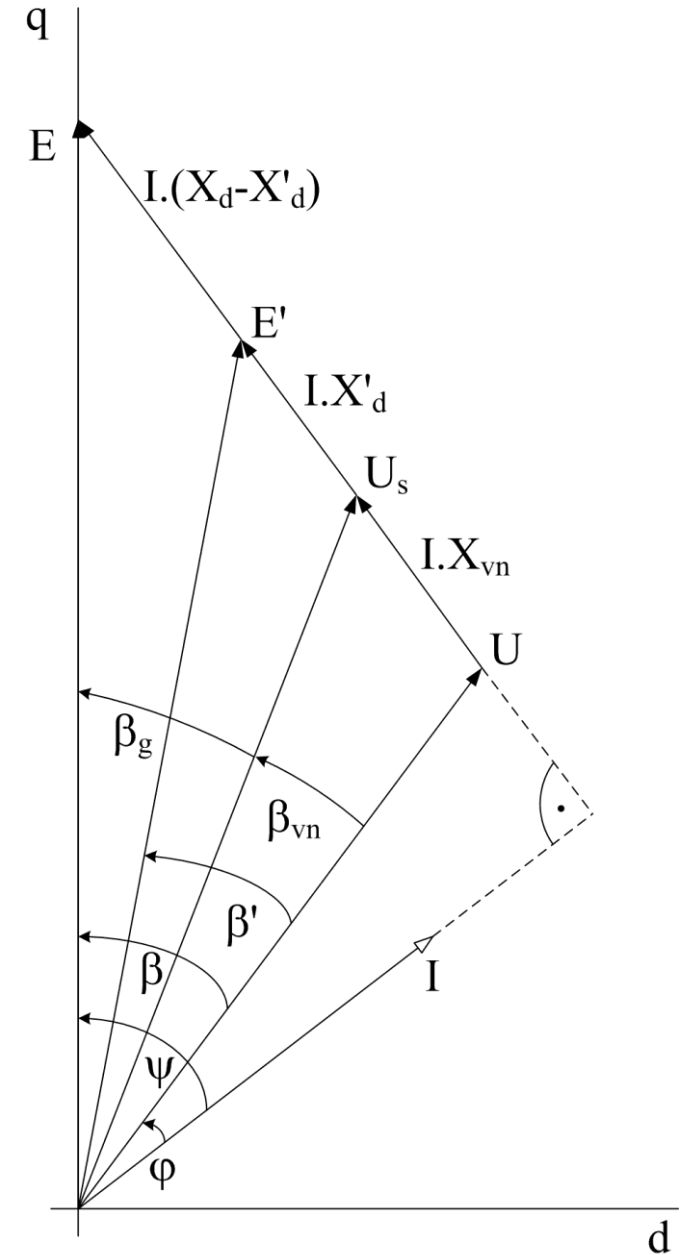
Alternator's power

$$P = \frac{E \cdot U}{X_{dc}} \sin \beta$$

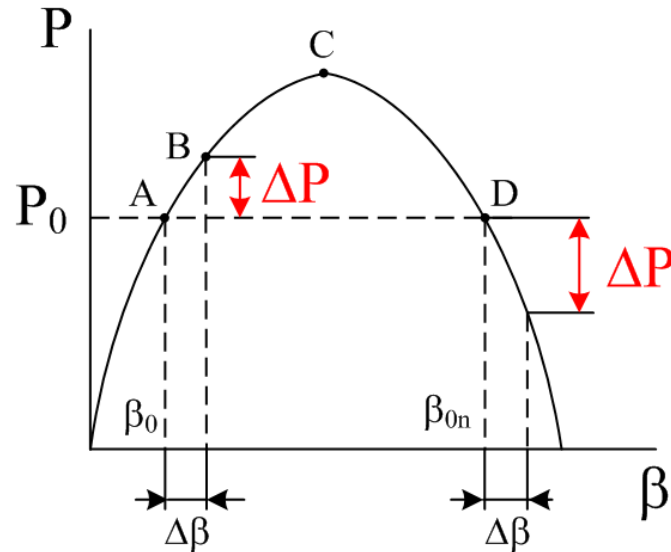
$$Q_i = \frac{E^2}{X_{dc}} - \frac{E \cdot U}{X_{dc}} \cos \beta$$

Valid for the infinite power system ($f, U = \text{const.}, X = 0$), constant source voltage (E), smooth-core rotor (turbo alternator).

Stability is influenced by transmitted power (P), source voltage (E) and transmission configuration (X) \rightarrow longitudinal compensation (C), higher source voltage



System steady-state stability



Stable state

$$P_0 = P_m$$

(electrical (generator) = mechanical (turbine), no losses)

$$\omega_0 = \textit{konst.} \text{ (system and machine)}$$

Mechanical power of turbine is a constant – doesn't depend on β but depends on ω (regulation P-f)

Point A: rotor acceleration $\rightarrow \Delta\beta \rightarrow (P_0 + \Delta P) \rightarrow P_{el} > P_{mech} \rightarrow$ rotor retardation \rightarrow stabilization \rightarrow point A is stable

Point D: rotor acceleration $\rightarrow \Delta\beta \rightarrow (P_0 - \Delta P) \rightarrow P_{el} < P_{mech} \rightarrow$ rotor acceleration \rightarrow loss of synchronism \rightarrow point D is unstable

Synchronization power

$$P_c = \frac{dP}{d\beta} = \frac{E \cdot U}{X_{dc}} \cos \beta$$

Stable area

$$P_c > 0$$

Steady-state stability limit

$$P_c = 0$$

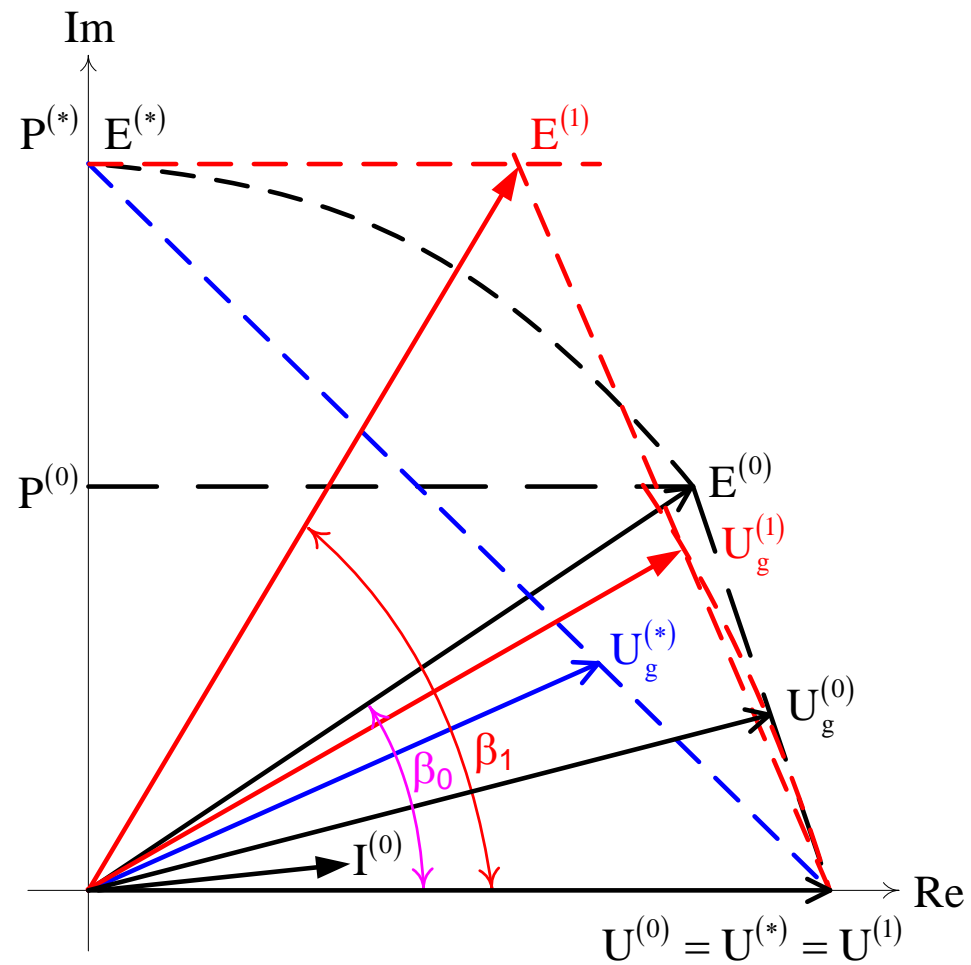
Coefficient of reserved power (usually above 20%)

$$k_P = \frac{P_m - P_0}{P_0}$$

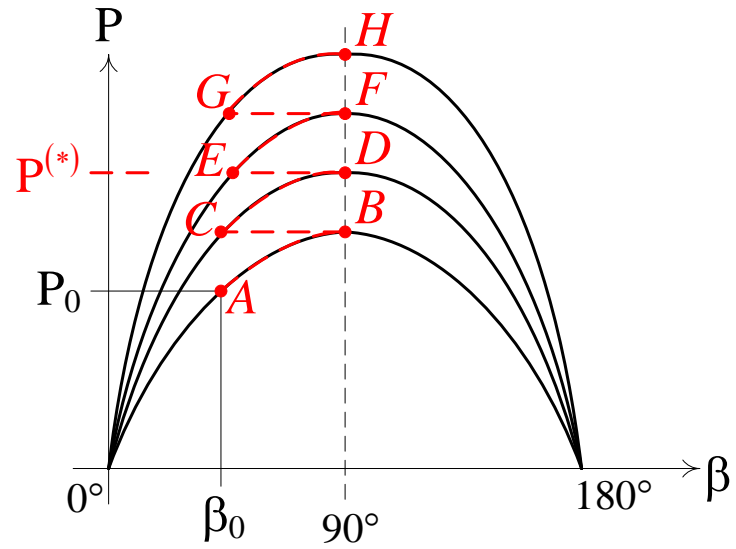
Note: More machines → need to watch P curve of each machine

Regulation of source voltage

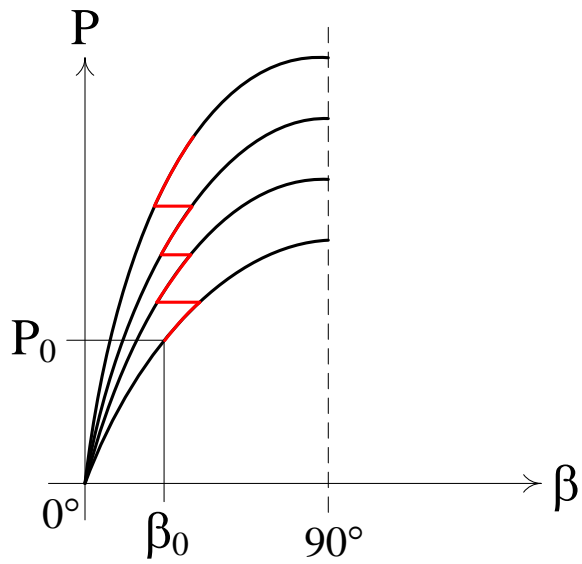
$$P = \frac{E \cdot U}{X_{dc}} \sin \beta = k \cdot E \cdot \sin \beta$$



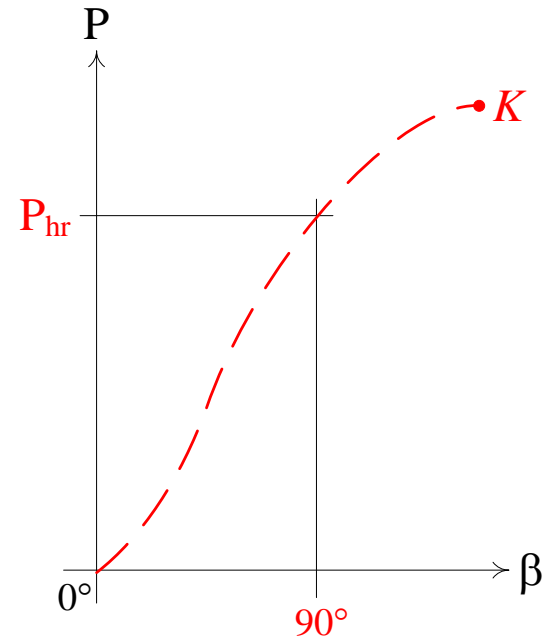
External characteristic →



→



→



Machine with salient poles

$$I \cdot X_q \cdot \cos \varphi = E_q \cdot \sin \beta$$

$$E_q = E - I_d \cdot (X_d - X_q)$$

$$I_d \cdot X_d = E - U_g \cos \beta$$

Modification

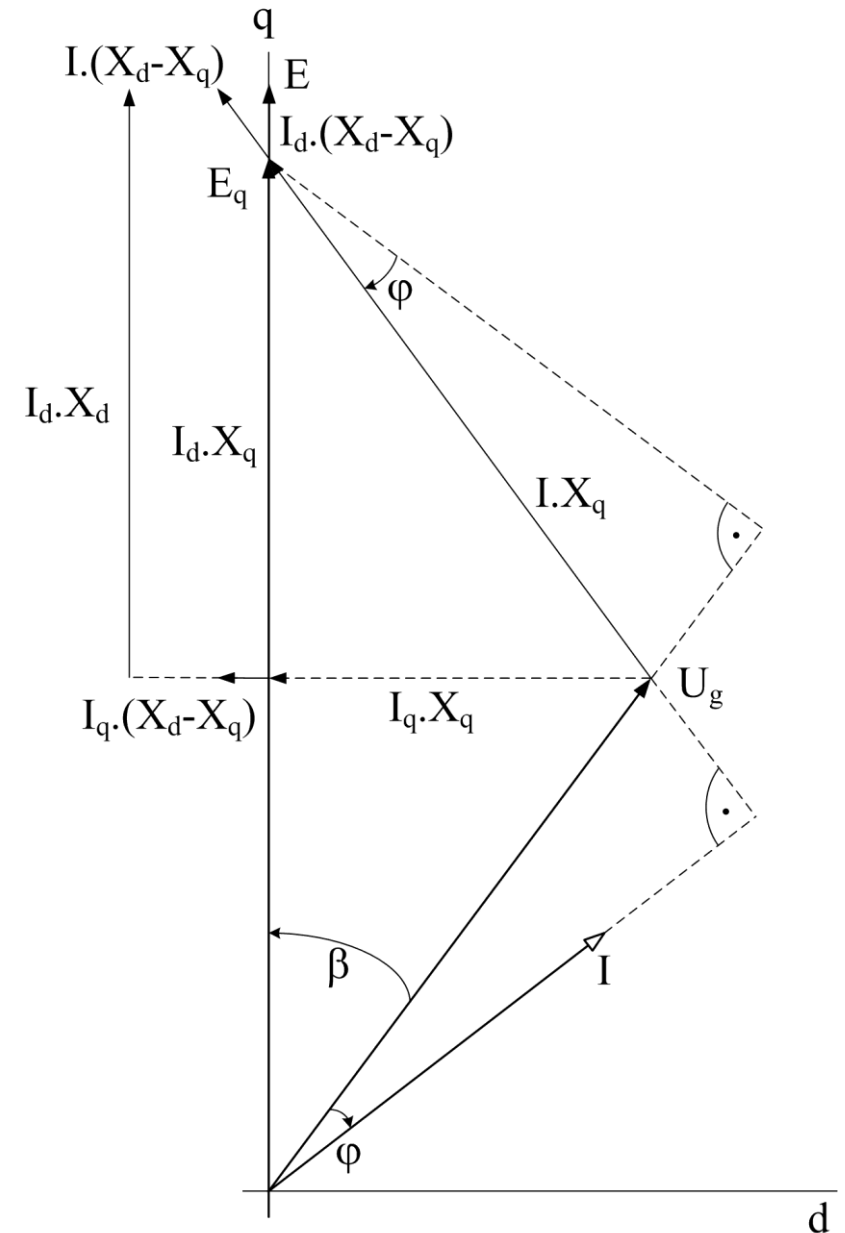
$$I_d = \frac{E}{X_d} - \frac{U_g}{X_d} \cos \beta$$

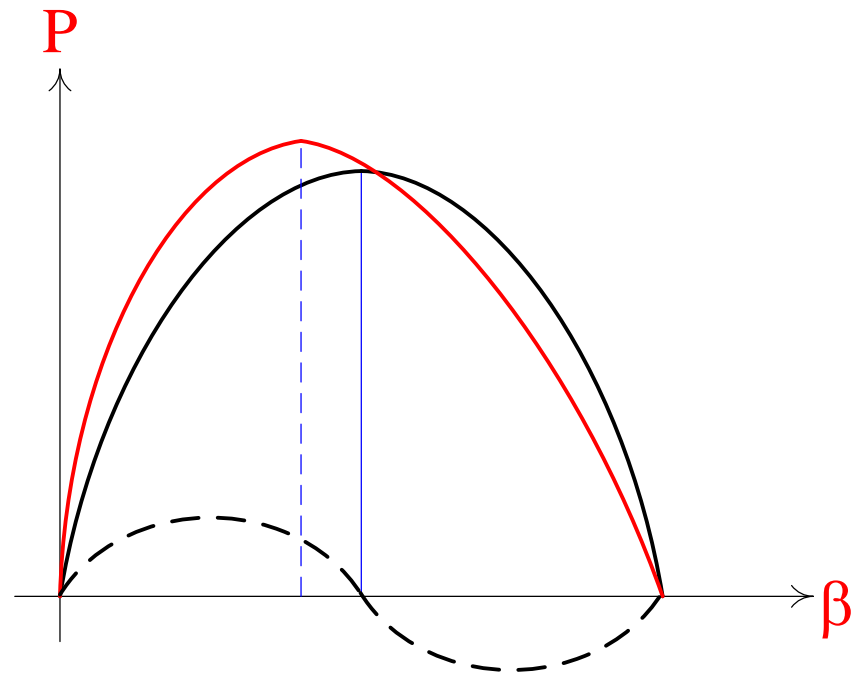
$$E_q = E \cdot \frac{X_q}{X_d} + U_g \cos \beta \cdot \frac{X_d - X_q}{X_d}$$

Generator power

$$P = U_g \cdot I \cdot \cos \varphi$$

$$P = \frac{E \cdot U_g}{X_d} \sin \beta + \frac{U_g^2}{2} \cdot \frac{X_d - X_q}{X_d X_q} \sin 2\beta$$





Generator to the network over series impedance

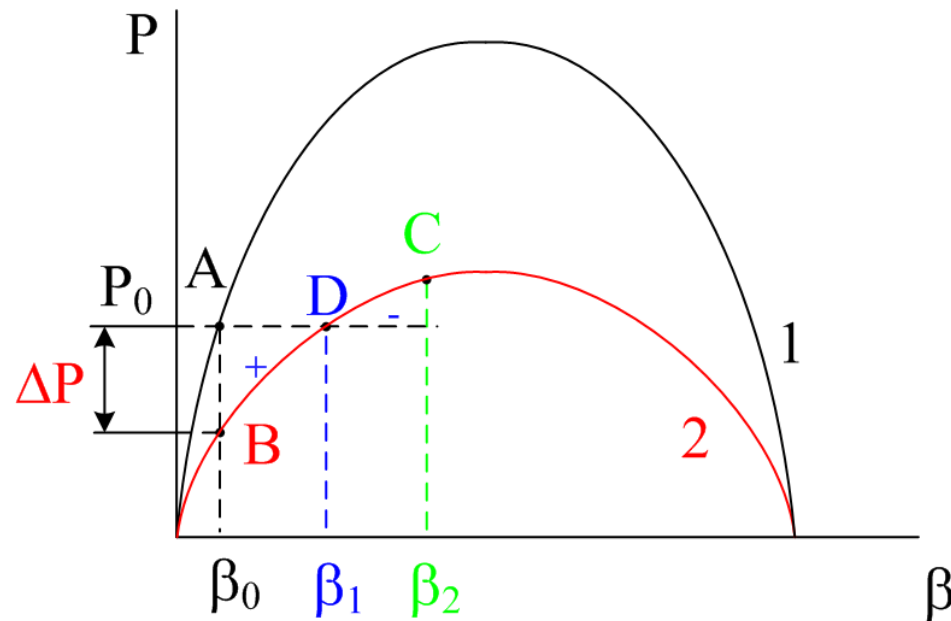
$$P = \frac{E \cdot U_g}{X_d + X_{vn}} \sin \beta + \frac{U_g^2}{2} \cdot \frac{X_d - X_q}{(X_d + X_{vn})(X_q + X_{vn})} \sin 2\beta$$

System transient stability

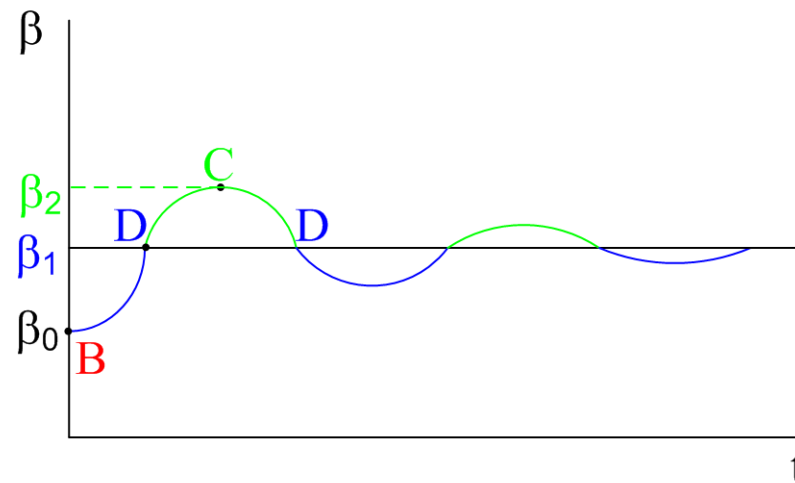
Parameters change in the system → impact to power changes → possible loss of stability.



$$X_2 > X_1$$



- Point A before the changes
- Inertia $\rightarrow \beta_0$ doesn't change suddenly \rightarrow generator power drops by ΔP
- $P_m - P_{el} =$ accelerating power
- In the point D $\omega > \omega_0 \rightarrow \beta$ grows up to the point C, gradual retardation
- Stabilization after several swings in the point D (a few seconds period)



The point C is too far (ΔP accelerating) \rightarrow loss of synchronism.

Behavior solution $\beta = f(t)$

Motion equation

$$W_k = \frac{1}{2} J \omega^2$$

$$P_a = P_m - P_e = \frac{dW_k}{dt} = \frac{1}{2} J 2\omega \frac{d\omega}{dt}$$

$P_a > 0$ - accelerating power

$P_a < 0$ - retarding power

Swing equation

$$P_m - \frac{E \cdot U}{X_{dc}} \sin \beta(t) = J \omega(t) \frac{d\omega(t)}{dt}$$

$$\omega(t) = \omega_0 + \frac{d\beta(t)}{dt}$$

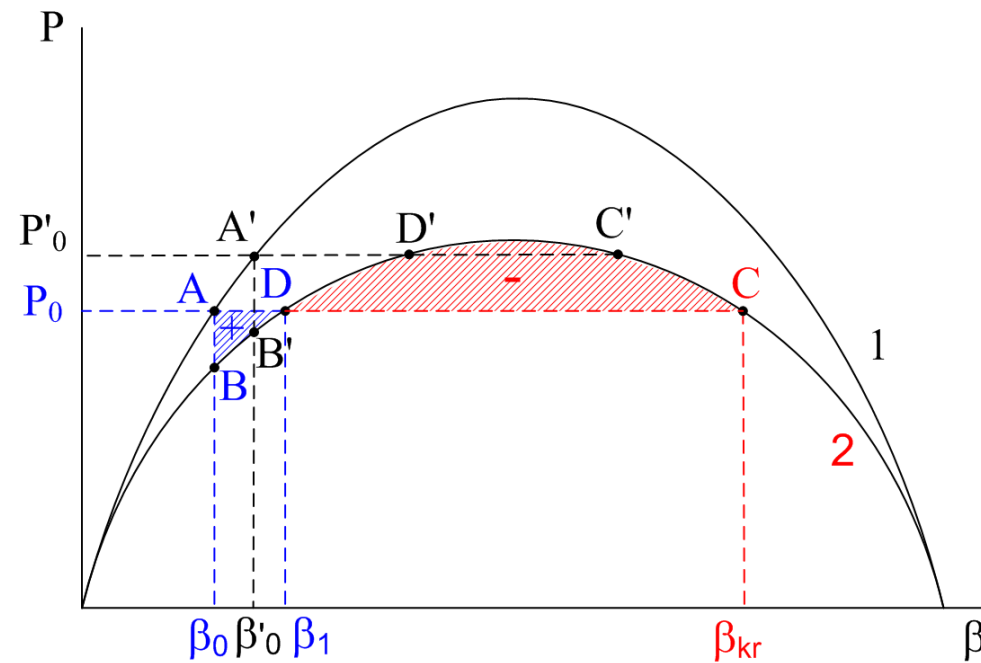
$$\beta(0) = \beta_0 ; \omega(0) = \omega_0$$

Inertia moment from start-up time

$$P = M\omega = J\varepsilon\omega \cong J \frac{\Delta\omega}{\Delta t} \omega = \frac{J\omega^2}{T}$$

$$J = \frac{T_m P_n}{\omega_0^2}$$

Equal areas method



Accelerating energy (area +)

$$A_a = \int_{\beta_0}^{\beta_1} (P_0 - P_{el}) d\beta$$

Retarding energy (area -)

$$A_r = \int_{\beta_1}^{\beta_{kr}} (P_{el} - P_0) d\beta$$

For keeping in synchronism

$$A_a \leq A_r$$

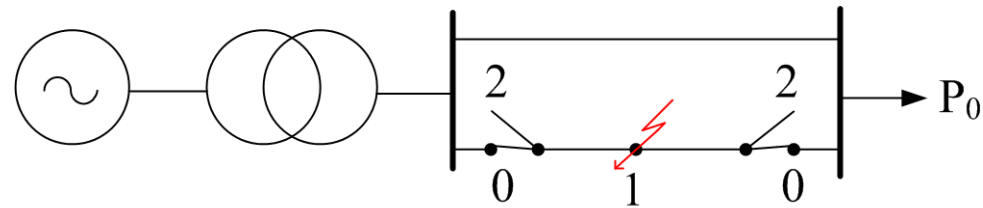
Transient stability

- limit at $A_a = A_r$, there is no strict angle limit
- during swing the angle can be $\beta > 90^\circ$

Auto-reclosing (AR)

During fault short-term disconnection and after a while repeated reclosing of the faulted section.

- temporary failure is disappeared → operation
- permanent failure → final disconnection



A_0 initial state
 $A_1 - B_1$ short-circuit
 B_1 short-circuit disconnecting
 $B_2 - C_2$ disconnected power line
 C_2 AR (successful)
 $C_3 - D_3$ swinging on the original characteristic

AR disconnecting time \sim between angles β_1 and β_2 (compromise between stability and arc burning).

