## STEADY STATES (LOAD FLOW) CALCULATIONS IN POWER SYSTEMS - Current loads

## Simple DC line (LV, MV)

Double-wire circuit. Assumption: constant cross-section and resistivity.
Single loads supplied from one side
Standard distribution lines.


## a) addition method

It adds voltage drops along the power line sections. (Voltage drops are always in both conductors in the section.)
$k^{\text {th }}$ section

$$
\mathrm{U}_{(\mathrm{k}-1)}-\mathrm{U}_{\mathrm{k}}=\Delta \mathrm{U}_{(\mathrm{k}-1) \mathrm{k}}=2 \frac{\rho}{\mathrm{~S}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \mathrm{I}_{(\mathrm{k}-1) \mathrm{k}} \quad\left(\mathrm{~V} ; \Omega \mathrm{m}, \mathrm{~m}^{2}, \mathrm{~m}, \mathrm{~A}\right)
$$

Current in $k^{\text {th }}$ section

$$
I_{(k-1) k}=\sum_{y=k}^{n} I_{y}
$$

Maximum voltage drop

$$
\Delta \mathrm{U}_{\mathrm{n}}=\sum_{\mathrm{k}=1}^{\mathrm{n}} \Delta \mathrm{U}_{(\mathrm{k}-1) \mathrm{k}}=2 \frac{\rho}{\mathrm{~S}} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \mathrm{I}_{\mathrm{y}}
$$

b) superposition method

It adds voltage drops for individual discrete loads:

$$
\Delta \mathrm{U}_{\mathrm{n}}=2 \frac{\rho}{\mathrm{~S}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \mathrm{I}_{\mathrm{k}}
$$

$1_{k} I_{k} \ldots$ current moments to the feeder
Relative voltage drop:

$$
\varepsilon=\frac{\Delta \mathrm{U}}{\mathrm{U}_{\mathrm{n}}}(-; \mathrm{V}, \mathrm{~V})
$$

Note. Losses must be calculated only by means of the addition method!

$$
\begin{aligned}
& \Delta \mathrm{P}_{(\mathrm{k}-1) \mathrm{k}}=2 \frac{\rho}{\mathrm{~S}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \mathrm{I}_{(\mathrm{k}-1) \mathrm{k}}^{2} \quad\left(\mathrm{~W} ; \Omega \mathrm{m}, \mathrm{~m}^{2}, \mathrm{~m}, \mathrm{~A}\right) \\
& \Delta \mathrm{P}=\sum_{\mathrm{k}=1}^{\mathrm{n}} \Delta \mathrm{P}_{(\mathrm{k}-1) \mathrm{k}}
\end{aligned}
$$

## Single loads supplied from both sides - the same feeders voltages




- Ring grid, higher reliability of supply.
- Two one-feeder lines after a fault. More often also in standard operation mode.
- Calculation of current distribution and voltage drops.

Consider $\mathrm{I}_{\mathrm{B}}$ as a negative load:

$$
\Delta \mathrm{U}_{\mathrm{AB}}=\mathrm{U}_{\mathrm{A}}-\mathrm{U}_{\mathrm{B}}=0=2 \frac{\rho}{\mathrm{~S}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \mathrm{I}_{\mathrm{k}}-2 \frac{\rho}{\mathrm{~S}} 1 \mathrm{I}_{\mathrm{B}}
$$

Hence (moment theorem)

$$
\mathrm{I}_{\mathrm{B}}=\frac{\sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \mathrm{I}_{\mathrm{k}}}{1}
$$

Analogous (current moments to other feeder)

$$
\mathrm{I}_{\mathrm{A}}=\frac{\sum_{\mathrm{k}=1}^{\mathrm{n}}\left(1-\mathrm{l}_{\mathrm{k}}\right) \mathrm{I}_{\mathrm{k}}}{1}
$$

Of course

$$
\mathrm{I}_{\mathrm{A}}+\mathrm{I}_{\mathrm{B}}=\sum_{\mathrm{y}=1}^{\mathrm{n}} \mathrm{I}_{\mathrm{y}}
$$

Current distribution identifies the place with the biggest voltage drop $=$ the place with feeder division $\rightarrow$ split-up into two one-feeder lines.


Single loads supplied from both sides - different feeders voltages
Two different sources, meshed grid.


Superposition:

1) Current distribution with the same voltages.
2) Different voltages and zero loads $\rightarrow$ balancing current

$$
\mathrm{I}_{\mathrm{v}}=\frac{\mathrm{U}_{\mathrm{A}}-\mathrm{U}_{\mathrm{B}}}{2 \frac{\rho}{\mathrm{~S}} 1}
$$

3) Sum of the solutions $1+2$


Further calculation is the same.
Or directly:

$$
\begin{aligned}
& \mathrm{U}_{\mathrm{A}}-\mathrm{U}_{\mathrm{B}}=2 \frac{\rho}{\mathrm{~S}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \mathrm{I}_{\mathrm{k}}-2 \frac{\rho}{\mathrm{~S}} 1 \mathrm{I}_{\mathrm{B}} \\
& \mathrm{I}_{\mathrm{B}}=\frac{2 \frac{\rho}{\mathrm{~S}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \mathrm{I}_{\mathrm{k}}}{2 \frac{\rho}{\mathrm{~S}} 1}-\frac{\mathrm{U}_{\mathrm{A}}-\mathrm{U}_{\mathrm{B}}}{2 \frac{\rho}{\mathrm{~S}} 1}
\end{aligned}
$$



## AC-3 phase power lines LV, MV

Series parameters are applied, for LV X $\rightarrow 0$.
3 phase power line MV, 1 load at the end
Symmetrical load $\rightarrow 1$ phase diagram, operational parameters.

Complex voltage drop


$$
\begin{aligned}
\Delta \hat{\mathrm{U}}_{\mathrm{ph}}= & \hat{\mathrm{Z}}_{\mathrm{l}} \hat{\mathrm{I}}=(\mathrm{R}+\mathrm{jX})\left(\mathrm{I}_{\mathrm{re}} \mp \mathrm{jI}_{\mathrm{im}}\right) \mathrm{CAP} \\
\Delta \hat{\mathrm{U}}_{\mathrm{ph}} & =\mathrm{RI}_{\mathrm{re}} \pm \mathrm{XI}_{\mathrm{im}}+\mathrm{j}\left(\mathrm{XI}_{\mathrm{re}} \mp \mathrm{RI}_{\mathrm{im}}\right) \mathrm{IND} \\
& \text { magnitude phase }
\end{aligned}
$$

Phasor diagram (input $\mathrm{U}_{\mathrm{ph} 2}, \mathrm{I}, \varphi_{2}$ ) (angle $v$ usually small, up to $3^{\circ}$ )

Imagin. part neglecting and modifications

$$
\Delta \mathrm{U}_{\mathrm{ph}}=\frac{\mathrm{R} 3 \mathrm{U}_{\mathrm{ph}} \mathrm{I}_{\mathrm{re}} \pm \mathrm{X} 3 \mathrm{U}_{\mathrm{ph}} \mathrm{I}_{\mathrm{im}}}{3 \mathrm{U}_{\mathrm{ph}}}=\frac{\mathrm{RP} \pm \mathrm{XQ}}{3 \mathrm{U}_{\mathrm{ph}}}
$$

Percentage voltage drop

$$
\varepsilon=\frac{\Delta \mathrm{U}_{\mathrm{ph}}}{\mathrm{U}_{\mathrm{ph}}}=\frac{\mathrm{RP} \pm \mathrm{XQ}}{3 \mathrm{U}_{\mathrm{ph}}^{2}}=\frac{\mathrm{RP} \pm \mathrm{XQ}}{\mathrm{U}^{2}}
$$

3 phase active power losses

$$
\begin{aligned}
\Delta \hat{\mathrm{S}} & =3 \Delta \hat{\mathrm{U}}_{\mathrm{ph}} \hat{\mathrm{I}}^{*}=3 \hat{\mathrm{Z}}_{\mathrm{I}} \hat{\mathrm{I}}^{\cdot} \cdot \mathrm{I}^{*}=3 \hat{\mathrm{Z}}_{\mathrm{I}} \mathrm{I}^{2}= \\
& =3(\mathrm{R}+\mathrm{jX}) \mathrm{I}^{2}=3 \mathrm{RI}^{2}+\mathrm{j} 3 \mathrm{XI} \mathrm{I}^{2} \\
\Delta \mathrm{P} & \left.=3 \mathrm{R} \mathrm{I}_{\mathrm{re}}^{2}+\mathrm{I}_{\mathrm{im}}^{2}\right) \quad(\mathrm{W} ; \Omega, \mathrm{A})
\end{aligned}
$$


! Even the reactive current (power) causes active power losses!

## 3 phase MV power line supplied from one side

Constant series impedance

$$
\hat{\mathrm{Z}}_{\mathrm{l}_{1}}=\mathrm{R}_{1}+\mathrm{j} \mathrm{X}_{1} \quad(\Omega / \mathrm{km})
$$



Voltage drop at the end (needn't be the highest one, it depends on load character)

- superposition

$$
\begin{aligned}
& \Delta \hat{\mathrm{U}}_{\mathrm{phAn}}=\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \hat{\mathrm{I}}_{\mathrm{k}} \\
& \Delta \hat{\mathrm{U}}_{\mathrm{phAn}}=\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(1_{\mathrm{k}}-1_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \hat{\mathrm{I}}_{\mathrm{y}}
\end{aligned}
$$

After imaginary part neglecting (addition)

$$
\begin{aligned}
& \Delta \mathrm{U}_{\mathrm{phAn}} \doteq \mathrm{R}_{1} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \mathrm{I}_{\mathrm{rek}} \pm \mathrm{X}_{1} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \mathrm{I}_{\mathrm{imk}} \text { IND } \\
& \Delta \mathrm{U}_{\mathrm{phAP}} \doteq \frac{\mathrm{R}_{1} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(\mathrm{l}_{\mathrm{k}}-1_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \mathrm{P}_{\mathrm{k}} \pm \mathrm{X}_{1} \sum_{\mathrm{k}=1}^{\mathrm{n}}\left(\mathrm{l}_{\mathrm{k}}-1_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \mathrm{Q}_{\mathrm{k}} \text { IND }}{3 \mathrm{U}_{\mathrm{ph}}} \text { CAP }
\end{aligned}
$$

Voltage drop up to the point X (not end)

- superposition

$$
\begin{aligned}
& \Delta \hat{\mathrm{U}}_{\mathrm{phAX}}=\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \sum_{\mathrm{k}=1}^{\mathrm{X}} 1_{\mathrm{k}} \hat{\mathrm{I}}_{\mathrm{k}}+\hat{\mathrm{Z}}_{\mathrm{l}_{1}} 1_{\mathrm{AX}} \sum_{\mathrm{k}=\mathrm{X}+1}^{\mathrm{n}} \hat{\mathrm{I}}_{\mathrm{k}} \\
& \Delta \hat{\mathrm{U}}_{\mathrm{phAX}}=\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \sum_{\mathrm{k}=1}^{\mathrm{X}}\left(\mathrm{l}_{\mathrm{k}}-\mathrm{l}_{(\mathrm{k}-1)}\right) \cdot \sum_{\mathrm{y}=\mathrm{k}}^{\mathrm{n}} \hat{\mathrm{I}}_{\mathrm{y}}
\end{aligned}
$$

3 phase MV power line supplied from both sides


Calculation as for DC line (feeder is a negative load, zero voltage drop).

$$
\Delta \hat{\mathrm{U}}_{\mathrm{phAB}}=0=\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \hat{\mathrm{I}}_{\mathrm{k}}-\hat{\mathrm{Z}}_{\mathrm{l}_{1}} \cdot \hat{\mathrm{I}}_{\mathrm{B}}
$$

Moment theorems

$$
\hat{I}_{B}=\frac{\sum_{\mathrm{k}=1}^{\mathrm{n}} 1_{\mathrm{k}} \hat{\mathrm{I}}_{\mathrm{k}}}{1} \quad \hat{\mathrm{I}}_{\mathrm{A}}=\frac{\sum_{\mathrm{k}=1}^{\mathrm{n}}\left(1-1_{\mathrm{k}}\right) \hat{\mathrm{I}}_{\mathrm{k}}}{1} \quad \hat{\mathrm{I}}_{\mathrm{A}}+\hat{\mathrm{I}}_{\mathrm{B}}=\sum_{\mathrm{y}=1}^{\mathrm{n}} \hat{\mathrm{I}}_{\mathrm{y}}
$$

(In principle it is the current divider for each load.)
Active and reactive current sign change could be in different nodes $\rightarrow$ maximum voltage drop should be checked in all grid points.


$$
\left.\Delta \hat{U}_{\text {phex }}=\hat{z}_{l_{k=x}}^{n} \sum_{k(k+1)}-I_{k}\right) \cdot \hat{\mathbf{I}}_{(k+1) k}=\hat{z}_{|l|} \sum_{k=x}^{n} l_{(k+1) k} \cdot \hat{\mathbf{I}}_{(k+1) k}
$$



## Meshed grids MV

## Bus voltage method

Grid with $n$ nodes. Set series branch parameters $\hat{\mathrm{Z}}_{\mathrm{km}}$, load currents (bus currents) $\hat{\mathrm{I}}_{\mathrm{k}}$, min. 1 bus voltage $\hat{\mathrm{U}}_{\text {phk }}$ (between the bus and the ground).


Calculation with series admittances

$$
\hat{\mathrm{Y}}_{\mathrm{km}}=\hat{\mathrm{Z}}_{\mathrm{km}}^{-1}=\frac{1}{R_{\mathrm{km}}+\mathrm{j} X_{\mathrm{km}}}
$$

Node $k$

$$
\begin{aligned}
& \hat{\mathrm{I}}_{\mathrm{k}}+\sum_{\substack{\mathrm{m}=1 \\
\mathrm{~m} \neq \mathrm{k}}}^{\mathrm{n}} \hat{\mathrm{I}}_{\mathrm{km}}+\hat{\mathrm{I}}_{\mathrm{k} 0}=0 \\
& \hat{\mathrm{I}}_{\mathrm{k} 0}=\hat{\mathrm{U}}_{\mathrm{phk}} \hat{\mathrm{Y}}_{\mathrm{k} 0}
\end{aligned}
$$

Branches $k, m$

$$
\hat{\mathrm{I}}_{\mathrm{km}}=\left(\hat{\mathrm{U}}_{\mathrm{phk}}-\hat{\mathrm{U}}_{\mathrm{phm}}\right) \hat{\mathrm{Y}}_{\mathrm{km}}
$$



After modifications:

$$
\hat{I}_{\mathrm{k}}=-\sum_{\substack{\mathrm{m}=1 \\ \mathrm{~m} \neq \mathrm{k}}}^{\mathrm{n}}\left(\hat{\mathrm{U}}_{\mathrm{phk}}-\hat{\mathrm{U}}_{\mathrm{phm}}\right) \hat{Y}_{\mathrm{km}}-\hat{\mathrm{U}}_{\mathrm{phk}} \hat{\mathrm{Y}}_{\mathrm{k} 0}
$$

$$
\hat{I}_{k}=-\hat{U}_{p h k}\left(\sum_{\substack{\mathrm{m}=1 \\ m \neq k}}^{\mathrm{n}} \hat{Y}_{\mathrm{km}}+\hat{Y}_{\mathrm{k} 0}\right)+\sum_{\substack{\mathrm{m}=1 \\ \mathrm{~m} \neq \mathrm{K}}}^{\mathrm{n}} \hat{U}_{\mathrm{pmm}} \hat{Y}_{\mathrm{km}}
$$

Admittance matrix parameters definition:
Bus self-admittance (diagonal element)

$$
\hat{\mathrm{Y}}_{(\mathrm{k}, \mathrm{k})}=-\sum_{\substack{\mathrm{m}=1 \\ \mathrm{~m} \neq \mathrm{k}}}^{\mathrm{n}} \hat{\mathrm{Y}}_{\mathrm{km}}-\hat{\mathrm{Y}}_{\mathrm{k} 0}
$$

Between buses admittance (non-diagonal element)

$$
\begin{aligned}
& \hat{\mathrm{Y}}_{(\mathrm{k}, \mathrm{~m})}=\hat{\mathrm{Y}}_{(\mathrm{m}, \mathrm{k})}=\hat{\mathrm{Y}}_{\mathrm{km}} \text { for } \mathrm{m} \neq \mathrm{k} \\
& \left(\text { for non-connected buses } \hat{\mathrm{Y}}_{(\mathrm{k}, \mathrm{~m})}=0\right)
\end{aligned}
$$

Hence

$$
\hat{\mathrm{I}}_{\mathrm{k}}=\sum_{\mathrm{m}=1}^{\mathrm{n}} \hat{\mathrm{Y}}_{(\mathrm{k}, \mathrm{~m})} \hat{\mathrm{U}}_{\mathrm{fm}}
$$

Matrix form

$$
(\hat{\mathrm{I}})=(\hat{\mathrm{Y}})\left(\hat{\mathrm{U}}_{\mathrm{ph}}\right)
$$

Set voltages at buses 1 to $k(x)$, currents at buses $k+1$ to $n(y)$

$$
\left.\left.\binom{\left(\hat{\mathrm{I}}_{\mathrm{x}}\right.}{\hat{\mathrm{I}}_{\mathrm{y}}}\right)=\left(\begin{array}{cc}
\left(\hat{\mathrm{Y}}_{\mathrm{xx}}\right) & \left(\hat{\mathrm{Y}}_{\mathrm{xy}}\right) \\
\left(\hat{\mathrm{Y}}_{\mathrm{xy}}\right)^{\mathrm{T}} & \left(\hat{\mathrm{Y}}_{\mathrm{yy}}\right)
\end{array}\right)\binom{\left(\hat{U}_{\mathrm{phx}}\right.}{\left(\hat{\mathrm{U}}_{\mathrm{phy}}\right.}\right)
$$

Hence

$$
\begin{aligned}
& \left(\hat{I}_{x}\right)=\left(\hat{Y}_{x x}\right)\left(\hat{U}_{p x}\right)+\left(\hat{Y}_{x y}\right)\left(\hat{U}_{p h y}\right) \\
& \left(\hat{I}_{y}\right)=\left(\hat{Y}_{x y}\right)^{T}\left(\hat{U}_{p h x}\right)+\left(\hat{\mathrm{Y}}_{\mathrm{yy}}\right)\left(\hat{U}_{\text {phy }}\right)
\end{aligned}
$$

Calculate $\left(\hat{\mathrm{I}}_{\mathrm{x}}\right),\left(\hat{\mathrm{U}}_{\text {phy }}\right)$

$$
\left(\hat{\mathrm{U}}_{\mathrm{phy}}\right)=\left(\hat{\mathrm{Y}}_{\mathrm{yy}}\right)^{-1}\left(\hat{\mathrm{I}}_{\mathrm{y}}\right)-\left(\hat{\mathrm{Y}}_{\mathrm{yy}}\right)^{-1}\left(\hat{\mathrm{Y}}_{\mathrm{xy}}\right)^{\mathrm{T}}\left(\hat{\mathrm{U}}_{\mathrm{phx}}\right)
$$

If some nodes are connected to the ground (through an admittance), then the admittance matrix is regular $\rightarrow$ to set all nodal current is enough.

$$
\left(\hat{\mathrm{U}}_{\mathrm{f}}\right)=(\hat{\mathrm{Y}})^{-1}(\hat{\mathrm{I}})
$$

Note 1: Similar for DC grid.

$$
(\mathrm{I})=(\mathrm{G})(\mathrm{U})
$$

Note 2: For power engineering - powers are set, currents are calculated from the powers.

$$
\hat{\mathrm{I}}=\left(\frac{\hat{\mathrm{S}}}{\sqrt{3} \hat{\mathrm{U}}}\right)^{*}
$$

Results are not precise if nominal voltages are used $\rightarrow$ iteration methods.

## HV lines

No load points.
Open-circuit

$$
\begin{aligned}
& \hat{\mathrm{I}}_{2}=0 \\
& \hat{\mathrm{U}}_{\mathrm{f} 10}=\hat{\mathrm{U}}_{\mathrm{f} 2} \cosh \hat{\gamma} \mathrm{l} \\
& \hat{\mathrm{I}}_{10}=\frac{\hat{\mathrm{U}}_{\mathrm{f} 2}}{\hat{\mathrm{Z}}_{\mathrm{v}}} \sinh \hat{\gamma} \mathrm{l}
\end{aligned}
$$

For ideal line

$$
\begin{aligned}
& \hat{\mathrm{U}}_{\mathrm{f} 10}=\hat{\mathrm{U}}_{\mathrm{f} 2} \cos \beta 1 \\
& \hat{\mathrm{I}}_{10}=\mathrm{j} \frac{\hat{\mathrm{U}}_{\mathrm{f} 2}}{\mathrm{Z}_{\mathrm{v}}} \sin \beta 1
\end{aligned}
$$

It is valid $\mathrm{U}_{\mathrm{f} 10} \leq \mathrm{U}_{\mathrm{f} 2} \rightarrow$ Ferranti effect Line character is like capacity.

Short-circuit

$$
\begin{aligned}
& \hat{\mathrm{U}}_{\mathrm{f} 2}=0 \\
& \hat{\mathrm{U}}_{\mathrm{f} 1}=\hat{\mathrm{Z}}_{\mathrm{v}} \hat{\mathrm{I}}_{2} \sinh \hat{\gamma} \mathrm{l} \\
& \hat{\mathrm{I}}_{1}=\hat{\mathrm{I}}_{2} \cosh \hat{\gamma} \mathrm{l}
\end{aligned}
$$

For ideal line

$$
\hat{\mathrm{U}}_{\mathrm{f} 1}=\mathrm{jZ} \hat{\mathrm{~V}}_{\mathrm{v}} \sin \beta 1
$$

$$
\hat{\mathrm{I}}_{1}=\hat{\mathrm{I}}_{2} \cos \beta 1
$$

Voltage decreases from the beginning to the end. Line character is like inductance.

## Example:

line $1 \times 400 \mathrm{kV}$ with two ground wires phase conductor: 3xACSR 450/52, ground wire: ACSR $185 / 31,1=300 \mathrm{~km}$ $\mathrm{R}_{1}=0,021 \Omega / \mathrm{km} ; \mathrm{X}_{1}=0,293 \Omega / \mathrm{km} ; \mathrm{G}_{1}=2 \cdot 10^{-8} \mathrm{~S} / \mathrm{km} ; \mathrm{B}_{1}=3,9 \cdot 10^{-6} \mathrm{~S} / \mathrm{km}$


Voltage level $\left(\mathrm{U}_{2}=400 \mathrm{kV}\right)$

$\mathrm{U}_{1}<\mathrm{U}_{\mathrm{n}}$ : Ferranti effect
$\mathrm{U}_{1} \sim \mathrm{U}_{\mathrm{n}}$ for $\mathrm{S}_{\mathrm{p}}$ area and $\cos \varphi=1$

## Transmission power factor

$\cos \varphi_{1}=\frac{\mathrm{P}_{1}}{\mathrm{~S}_{1}}$

open-circuit $\rightarrow$ line is like capacitive load higher power $\rightarrow$ line „self-compensation"

Line reactive power


## Line losses

$=$ open-circuit $\sim \mathrm{U}^{2}+$ load $\sim \mathrm{I}^{2}$

$\Delta P(M W)$


## Transmission efficiency

$\eta=\frac{P_{2}}{P_{1}}$

maximum for low powers for higher powers a flat curve

