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In[47]:= Quiet@Remove["Global`*"];  
$HistoryLength = 2;  
Off[FindRoot::lstol];  
SetDirectory[NotebookDirectory[]];
```

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In[51]:= mm = 0.001;  
cm = 10. mm;  
imax = 7;  
jmax = 12;  
TavstupZadane = 99.1;  
TbvstupZadane = 10.4;  
msteckouA = 5.23;  
msteckouB = 3.869;  
delkaVymeniku = 5.5;
```

In[60]:=

```

ClearAll[yjm, x, rceKruh, yjmax, kmax, udaje, Δyj, km, Δyjm];
D1 = 0.5; (*vnitrni prumer trouby B*)
d1 = 1.5 cm; (*vnitrni prumer trubicky A*)
t = 2 mm; (*tloustka streny trubicky A*)
ξy = 1.2; (*Δytrubicka+mezera=ξy*Δytrubicka*)
ξyukr = 2; (*kolikrat je mezera u kraje mensi, nez mezera mezi trubkami*)
ξxj1 = 0.2; (*kolikrat je pocatecni x vuci prumeru*)
Δytrubicka = d1 + 2 t;
ΔyjZadane = ξy * Δytrubicka;
Δyukr = ξyukr * (ΔyjZadane - Δytrubicka);
xj1 = ξxj1 * D1;

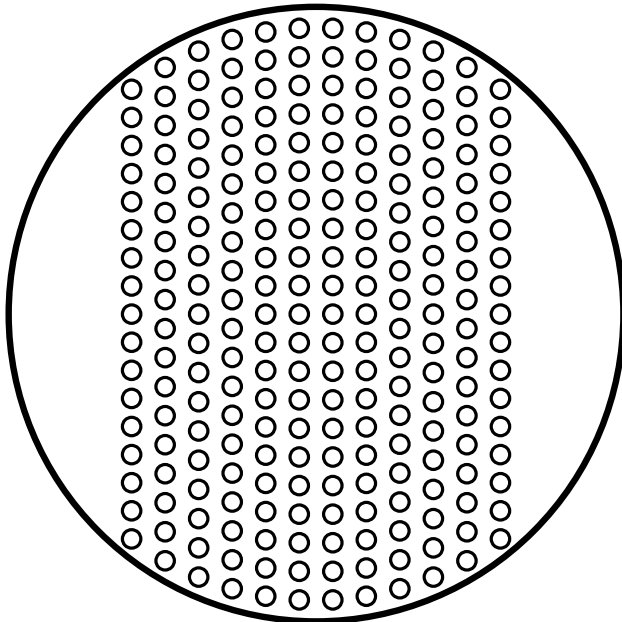
$$\Delta x = \frac{D1 - 2 xj1}{j_{\max} - 1};$$

x[j_Integer] := xj1 + (j - 1) * Δx;
rceKruh[x_, y_] := (x - 0.5 D1)2 + y2 == (0.5 D1)2;
yjmax[j_Integer] := yjm /. Solve[rceKruh[x[j], yjm]][[2]];
kmax[j_Integer] := Floor[km /. Solve[
  2 * yjmax[j] == 2 * Δyukr + km * Δytrubicka + (km - 1) * (ΔyjZadane - Δytrubicka), km][[1]]];
udaje[j_Integer, k_Integer] := Module[{km, yjm, prutocnaDelka},
  km = kmax[j];
  yjm = yjmax[j];
  Δyj = Δyjm /.
    Solve[2 * yjm == 2 * Δyukr + km * Δytrubicka + (km - 1) * (Δyjm - Δytrubicka), Δyjm][[1]];
  prutocnaDelka = 2 * Δyukr + (km - 1) * (Δyj + -Δytrubicka);

  {{x[j], -yjm + Δyukr + 0.5 * Δytrubicka + (k - 1) * Δyj}, {km, yjm, prutocnaDelka}, {j, k}}
];
kruh[{{x_, y_}, r_}, tk_, barva_] := Graphics[{Thickness[tk], barva, Circle[{x, y}, r]}];
stredy = Union@Flatten[Table[udaje[j, k][[1]], {j, jmax}, {k, kmax[j]}], 1];
kruh1 = kruh[{#, 0.5 d1}, 0.005, Black] & /@ stredy;
kruh2 = kruh[{{0.5 D1, 0}, 0.5 D1}, 0.01, Black];
grRez = Show[kruh1, kruh2]

```

Out[81]=



```

In[82]:= ClearAll[prutocnaDelka, SoutVrstva, SinVrstva,
    SkB, nyA, Tolej, gzA, nuA, vmaxB, αA, αB, nuB, kspom];
λTrubka = 41.5;
nTrubekA = Length[stredy];
SkA = nTrubekA * Pi *  $\frac{d1^2}{4}$ ;
Δz =  $\frac{\text{delkaVymeniku}}{\text{imax}}$ ;
RthTrubka =  $\frac{1}{2. * \text{Pi} * \lambda \text{Trubka} * \Delta z} * \text{Log}\left[\frac{d1 + 2 t}{d1}\right]$ ;
SvittrniTrubka = 2. * Pi * Δz * d1;
SvnejsiTrubka = 2. * Pi * Δz * (d1 + 2 t);
SinVrstva[j_] := SvittrniTrubka * kmax[j];
SoutVrstva[j_] := SvnejsiTrubka * kmax[j];
prutocnaDelka[j_] := udaje[j, 1][[-2, -1]];
SkB[j_] := prutocnaDelka[j] * Δz;
nyA[Tolej_] = N[<< "nyA"];
nyB = 10-6 * (<< "milionnyB")[#] &; (*funkce teploty A*)
cpA[T_] := 1988 + 0.01 T;
cpB[T_] := 4178 - 0.0478 T;
λA[T_] := 0.13141 + 0.0001 T;
λB = << "lambdaB"; (*funkce teploty B*)
PrA[Tolej_] = << "prA";
PrB = << "prB"; (*funkce teploty B*)
roA[T_] := 847 - 0.0000158 T;
roB[T_] := 1000 - 0.00047 T;
gzA[reA_, prA_, z_] :=  $\frac{\text{reA} * \text{prA} * d1}{z}$ ;
nuA[gz_, PrA_, Prw_] :=
     $\left(1 + 0.01 * \left(\frac{\text{PrA}}{\text{Prw}}\right)^{0.25}\right) * \text{Which}\left[0 \leq \text{gz} < 667, 4.364 + 0.263 * \text{gz}^{0.506} * \text{Exp}\left[\frac{-41.}{\text{gz}}\right],\right.$ 
 $\left.667 \leq \text{gz} < 2 * 10^4, 1.302 * \text{gz}^{0.333} - 0.5, \text{gz} \geq 2 * 10^4, 1.302 * \text{gz}^{0.333} - 1\right]$ ;
DcharB = d1 + 2 t;
vmaxB[j_, T_] :=  $\frac{\text{msteckouB}}{\text{roB}[T] * \text{SkB}[j]}$ ;
vA[T_] :=  $\frac{\text{msteckouA}}{\text{roA}[T] * \text{SkA}}$ ;
reA[T_] :=  $\frac{\text{vA}[T] * d1}{\text{nyA}[T]}$ ;
reB[T_, j_] :=  $\frac{\text{vmaxB}[j, T] * (d1 + 2 t)}{\text{nyB}[T]}$ ;

```

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αA[{{αAminule_, αBminule_}, {TAminule_, TBminule_}, z_}] :=
Module[{Tstena, Tdef, nu, re, pr, prw, gz, λ},
  Tstena = 
$$\frac{TAminule \alphaAminule + TBminule \alphaBminule}{\alphaAminule + \alphaBminule};$$

  Tdef = 0.5 * (Tstena + TAminule);
  re = reA[Tdef];
  pr = PrA[Tdef];
  prw = PrA[Tstena];
  gz = gzA[re, pr, z];
  nu = nuA[gz, pr, prw];
  λ = λA[Tdef];
  
$$\frac{nu * \lambda}{d1}$$

];

nuB[re_, PrB_, Prw_] := PrB0.36 *  $\left(\frac{PrB}{Prw}\right)^{0.25}$  * 0.52 re0.5;
(*0.25 kapaliny, 0, plyny, HeatTransfer str. 382*)
αB[{{αAminule_, αBminule_}, {TAminule_, TBminule_}, j_}] :=
Module[{Tstena, Dchar, Tdef, prB, prw, nu, re, λ},
  Tstena = 
$$\frac{TAminule \alphaAminule + TBminule \alphaBminule}{\alphaAminule + \alphaBminule};$$

  Dchar = d1 + 2 t;
  Tdef = 0.5 * (Tstena + TBminule);
  prB = PrB[Tdef];
  prw = PrB[Tstena];
  re = reB[Tdef, j];
  nu = nuB[re, prB, prw];
  λ = λB[Tdef];
  
$$\frac{nu * \lambda}{d1 + 2 t}$$

];

kspom[{{αAminule_, αBminule_}, {TAminule_, TBminule_}, {j_, z_}}] :=
Module[{α1, α2, S1, S2},
  α1 = αA[{{αAminule, αBminule}, {TAminule, TBminule}, z}];
  S1 = SinVrstva[j];
  S2 = SoutVrstva[j];
  α2 = αB[{{αAminule, αBminule}, {TAminule, TBminule}, j}];

```

$$\frac{1}{RthTrubka + \frac{1}{\alpha_1 s_1} + \frac{1}{\alpha_2 s_2}}$$

```

];

ClearAll[doskSij];
doskSij[{i_Integer, j_Integer, res_}, dosalfas_] :=
Module[{aNew, aBNew, TAminule, TBminule, z, aAminule, aBminule},
{aAminule, aBminule} = {a[i, j], ab[i, j]} /. dosalfas;
z = Δz * (0.5 + i - 1);
TAminule = 0.5 * (Tain[i, j] + Taout[i, j]) /. res;
TBminule = Tbin[i, j] /. res;
aNew = aA[{aAminule, aBminule}, {TAminule, TBminule}, z];
aBNew = aB[{aAminule, aBminule}, {TAminule, TBminule}, j];
{{kS[i, j] -> kspom[{aNew, aBNew}, {TAminule, TBminule}, {j, z}]},
{mca[i, j] ->  $\frac{msteckouA * kmax[j]}{nTrubekA} * cpA[TAminule],$ 
mcb[i, j] -> msteckouB * cpB[TBminule]}}}, {a[i, j] -> aNew, ab[i, j] -> aBNew}}
];

```

ln[117]:=

```

ClearAll[rcebilanceLn, rcebilance];
rcebilanceLn[i_Integer, j_Integer] := {mca[i, j] * (Tain[i, j] - Taout[i, j]) = Q[i, j],
mcb[i, j] * (Tbout[i, j] - Tbin[i, j]) = Q[i, j],
kS[i, j] * (Tain[i, j] - Taout[i, j]) *
Log[Abs[ $\left(\frac{Tain[i, j] - Tbin[i, j]}{Taout[i, j] - Tbin[i, j]}\right)^{-1}$ ]] = Q[i, j]
};
rcebilance[i_Integer, j_Integer] := {mca[i, j] * (Tain[i, j] - Taout[i, j]) = Q[i, j],
mcb[i, j] * (Tbout[i, j] - Tbin[i, j]) = Q[i, j],
kS[i, j] * (0.5 * (Tain[i, j] + Taout[i, j]) - Tbin[i, j]) = Q[i, j]
};
rceSpojA[i_Integer, j_Integer] := {Taout[i, j] = Tain[i + 1, j]};
rceSpojB[i_?EvenQ, j_Integer] := {Tbout[i, j] = Tbin[i, j + 1]};
rceSpojB[i_?OddQ, j_Integer] := {Tbin[i, j] = Tbout[i, j + 1]};
rceSpojDole[i_?OddQ] := {Tbin[i, jmax] = Tbout[i + 1, jmax]};
rceSpojDole[i_?EvenQ] := {};
rceSpojNahore[i_?EvenQ] := {Tbin[i, 1] = Tbout[i + 1, 1]};
rceSpojNahore[i_?OddQ] := {};
rceVystupA = {Sum[mca[imax, j] * Taout[imax, j], {j, 1, jmax}] =
Tavystup * Sum[mca[imax, j], {j, 1, jmax}]};
rceVstupA[j_] := {Tain[1, j] = Tavstup};
rceVstupB = If[OddQ[imax], {Tbin[imax, jmax] = Tbvstup}, {Tbin[imax, 1] = Tbvstup}];
rceVystupB = {Tbout[1, 1] = Tbvystup};

```

```

In[131]:= r1 = Flatten[Table[rcebilance[i, j], {i, imax}, {j, jmax}]];
r1Ln = Flatten[Table[rcebilanceLn[i, j], {i, imax}, {j, jmax}]];
r2 = Flatten[Table[rceSpojA[i, j], {i, imax - 1}, {j, jmax}]];
r3 = Flatten[Table[rceSpojB[i, j], {i, imax}, {j, jmax - 1}]];
r4 = Flatten[Table[rceSpojDole[i], {i, imax - 1}]];
r4 = Flatten[Table[rceSpojNahore[i], {i, imax - 1}]];
r5 = Flatten[Table[rceSpojDole[i], {i, imax - 1}]];
r6 = Flatten[Table[rceVstupA[j], {j, jmax}]];
r7 = rceVystupA;
r8 = rceVstupB;
r9 = rceVystupB;
rdohr =
  Union@DeleteCases[Flatten[Union[ToExpression["r" <> ToString[#]] & /@ Range[9]], {}];
rdohrLn = Union[r1Ln, DeleteCases[
  Flatten[Union[ToExpression["r" <> ToString[#]] & /@ Range[2, 9, 1]], {}]];

In[144]:= mcbStart = msteckouB * cpB[TbvstupZAdane];
mcaStart = msteckouA *  $\frac{k_{\max}[\text{Round}[0.5 * j_{\max}]]}{n_{\text{TrubekA}}}$  * cpA[TavstupZadane];
ksStart = kspom[{{100, 100},
  {TavstupZadane, TbvstupZAdane}, {Round[0.5 * jmax], 0.5 * delkaVymeniku}}];

dosalfasStart =
  Flatten[Table[{a[i, j] -> 2 * ksStart, ab[i, j] -> 2 * ksStart}, {i, imax}, {j, jmax}]];

In[148]:= dosTry = {mcb[_] -> mcbStart, mca[_] -> mcaStart,
  ks[_] -> ksStart, Tavstup -> TavstupZadane, Tbvstup -> TbvstupZAdane};
rdos = rdohr /. dosTry;
nezname = Union[Cases[rdos, _[_Integer, _Integer], {0, ∞}], {Tavystup, Tbvystup}];
resStart = Solve[rdos, nezname][[1]];

In[152]:= ClearAll[dos];
dos[{res_, doslast_}] := Union[{Tavstup -> TavstupZadane, Tbvstup -> TbvstupZAdane},
  Flatten[Table[doskSij[{{i, j, res}, doslast}], {i, imax}, {j, jmax}]]];
dosStart = dos[{resStart, dosalfasStart}];

```

```

In[155]:= ClearAll[krokLin, krokLinLn, krokLn, krok];
krokLin[{doslast_, res_, iter_Integer}] := Module[{resNew},
  resNew = Solve[rdohr /. doslast, nezname][[1]];
  {dos[{resNew, doslast}], resNew, iter + 1}

];

krokLinLn[{doslast_, res_, iter_Integer}] :=
Module[{resNew, dosNew, rdohrNew, obory, resLn},
  resNew = Solve[rdohr /. doslast, nezname][[1]];
  dosNew = dos[{resNew, doslast}];
  rdohrNew = rdohrLn /. dosNew;
  obory = resNew /. (a_ -> b_) -> {a, b};
  resLn = FindRoot[rdohrNew, obory];
  {dos[{resLn, dosNew}], resLn, iter + 1}
];

krokLn[{doslast_, res_, iter_Integer}] :=
Module[{resNew, dosNew, rdohrNew, obory, resLn},
  rdohrNew = rdohrLn /. doslast;
  obory = res /. (a_ -> b_) -> {a, b};
  resLn = FindRoot[rdohrNew, obory];
  {dos[{resLn, doslast}], resLn, iter + 1}
];

krok[par : {doslast_, res_, iter_Integer}] :=
Which[iter < 2, krokLin[par], 2 ≤ iter < 3, krokLinLn[par], iter ≥ 3, krokLn[par]];

In[160]:= ClearAll[tav];
tav[{doslast_, res_, iter_Integer}] := Tavystup /. res;
dats = NestList[krok, {dosStart, resStart, 1}, 4];
{dosVys, resVys, iterVys} = dats[[-1]];
dosvys = Union[dosVys, resVys];
tav /@ dats
% - Last[%]

Out[165]= {61.9181, 59.4658, 59.5422, 59.5421, 59.5421}

Out[166]= {2.37605, -0.0762429, 0.000112176, 6.13069 × 10-7, 0.}

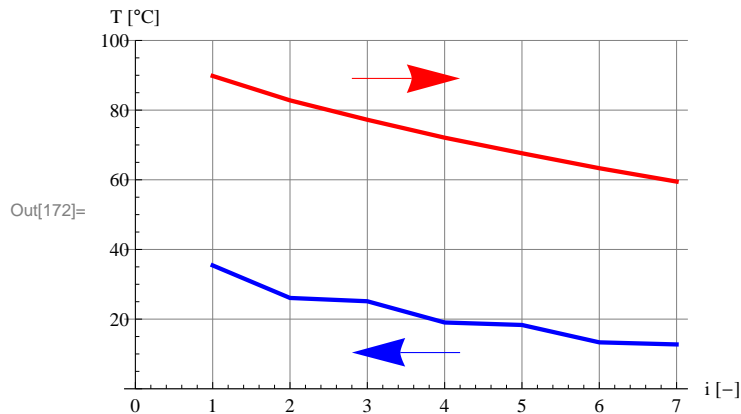
```

```

In[167]:= pla = ListPlot[({#, Taout[#, 2]} & /@ Range[imax]) /. dosvys, PlotRange → All, Joined → True,
  PlotStyle → {Thick, Red}, GridLines → Automatic, AxesLabel → {"i [-]", "T [°C]"}];
plb = ListPlot[({#, Tbout[#, 2]} & /@ Range[imax]) /. dosvys, PlotRange → All,
  Joined → True, PlotStyle → {Thick, Blue}, GridLines → Automatic];

sipka[barva_, {{x1_, y1_}, {x2_, y2_}}] :=
  Graphics[{barva, {Arrowheads[Large], Arrow[{x1, y1}, {x2, y2}]}}];
s1 = sipka[Red, {{0.4 * imax, Tavstup - 10}, {0.6 imax, Tavstup - 10}}] /. dosvys;
s2 = sipka[Blue, {{0.6 * imax, Tbvstup}, {0.4 imax, Tbvstup}}] /. dosvys;
Show[pla, plb, s1, s2, PlotRange → {Automatic, {0, 100}}, AxesOrigin -> {0, 0}]

```



```

In[173]:= vykon1 = Plus @@ (Union[Cases[resVys, Q[_Integer, _Integer], {0, ∞}]] /. dosvys);
vykon2 = (Tavstup * msteckouA * cpA[Tavstup] - Tavystup * Sum[mca[imax, j], {j, 1, jmax}]) /.
  dosvys;
vykon3 = (mcb[1, jmax] * Tbvystup - msteckouB * cpB[Tbvstup] * Tbvstup) /. dosvys;
{vykon1, vykon2, vykon3}
{{Tavstup - Tavystup, Tbvystup - Tbvstup}, {Tavystup, Tbvstup}} /. dosvys

```

Out[176]= {411 457., 411 615., 411 388.}

Out[177]= {{39.5579, 25.4608}, {59.5421, 35.8608}}